

**Architecture and Hardware Design of Lossless Compression Algorithms for  
Direct-Write Maskless Lithography Systems**

by

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University of California, Berkeley

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## Abstract

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Future lithography systems must produce chips with smaller feature sizes, while maintaining throughput comparable to today's optical lithography systems. This places stringent data handling requirements on the design of any direct-write maskless system. To achieve the throughput of one wafer layer per minute with a direct-write maskless lithography system, using 22 nm pixels for 45 nm technology, a data rate of 12 Tb/s is required. A recently proposed datapath architecture for direct-write lithography systems shows that lossless compression could play a key role in reducing the system throughput requirements. This architecture integrates low complexity hardware-based decoders with the writers, in order to decode a compressed rasterized layout in real time. To this end, a spectrum of lossless compression algorithms have been developed for rasterized integrated circuit (IC) layout data to provide

a tradeoff between compression efficiency and hardware complexity. In this thesis, I extend Block Context Copy Combinatorial Code (Block C4), a previously proposed lossless compression algorithm, to Block Golomb Context Copy Code (Block GC3), in order to reduce the hardware complexity, and to improve the system throughput. In particular, the hierarchical combinatorial code in Block C4 is replaced by Golomb run-length code to result in Block GC3. Block GC3 achieves minimum compression efficiency of 6.5 for  $1024 \times 1024$ , 5-bit Poly layer layouts in 130 nm technology. Even though this compression efficiency is 15% lower than that of Block C4, Block GC3 decoder is 40% smaller in area than Block C4 decoder.

In this thesis, I also illustrate hardware implementation of Block GC3 decoder with FPGA and ASIC synthesis flow. For one Block GC3 decoder with  $8 \times 8$  block size, 3233 slice flip-flops and 3086 4-input LUTs are utilized in a Xilinx Virtex II Pro 70 FPGA, corresponding to 4% of its resources. The decoder has 1.7 KB internal memory, which is implemented with 36 block memories, corresponding to 10% of the FPGA resources. The system runs at 100 MHz clock rate, with the overall output rate of 495 Mb/s for a single decoder. The corresponding ASIC implementation results in a  $0.07 \text{ mm}^2$  design with the maximum output rate of 2.47 Gb/s.

I also explore the tradeoff between encoder complexity and compression efficiency, with a case study for reflective E-beam lithography (REBL) system. In order to accommodate REBL's rotary writing system, I introduce Block RGC3, a variant of Block GC3, in order to adapt to the diagonal repetition of the rotated layout images. By increasing the encoding

complexity, Block RGC3 achieves minimum compression efficiency of 5.9 for  $256 \times 2048$ , 5-bit Metal-1 layer layouts in 65 nm technology with 40 KB buffer; this outperforms Block GC3 and all existing lossless compression algorithms, while maintaining a simple decoder architecture.

To my family,  
for their help and support along the way.

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# Chapter 1

## Introduction

### 1.1 Introduction to Maskless Lithography

This thesis presents the lossless data compression algorithm implementation for direct-write lithography systems. Lithography, the process of printing layout patterns on the wafer for semiconductor manufacturing, has traditionally been done by photolithography. In photolithography, the layout pattern, which is printed on a transparent or reflective optical mask, is projected onto the wafer by an overhead optical source. As future lithography systems produce chips with smaller feature sizes, such a method, creates some difficult challenges. According to international technology roadmap for semiconductors (ITRS) lithography 2009, one of the challenges is to fabricate cost-effective masks [21]. For the technologies beyond 45 nm, the cost and the defect-control issues of the mask, especially for extreme ultra-violet (EUV) lithography and double patterning, become more and more intractable, hence rising



the new lithography paradigm of maskless lithography.

The scenario of maskless lithography is simple: Rather than using a different mask for each layer, the writing system has a pixelated pattern generator which creates the layout pattern dynamically. The analogy of the maskless lithography is the digital light processing (DLP) technology used in projectors and televisions today [20]. However, the data throughput of maskless lithography is three orders of magnitude greater than today's high-definition video coding standards. Moreover, the micromirror devices of maskless lithography are smaller than those of the DLP, and are designed for direct-write lithography sources such as EUV and electron-beam (E-beam).

## 1.2 The Architecture of Maskless Lithography Systems

Figure 1.1 shows the architecture of an optical maskless lithography system [35] [29]. A similar architecture for the E-beam lithography can be found in the literature [33]. In this architecture, the optical source flashes on a writer system, which consists of a micromirror array and a writer control chip underneath it, and the patterns on the mirror array are reflected to the wafer on the scanning wafer stage. As the stage moves, the writer system has to provide different layout patterns for different portions of the wafer, and the data is transmitted from external storage devices to the writer system. Due to the physical dimension constraints of the micromirror array and writer system, an entire wafer can be written in a few thousands of such flashes.

In this scenario, the writer system controls the movement of every mirror in the mi-

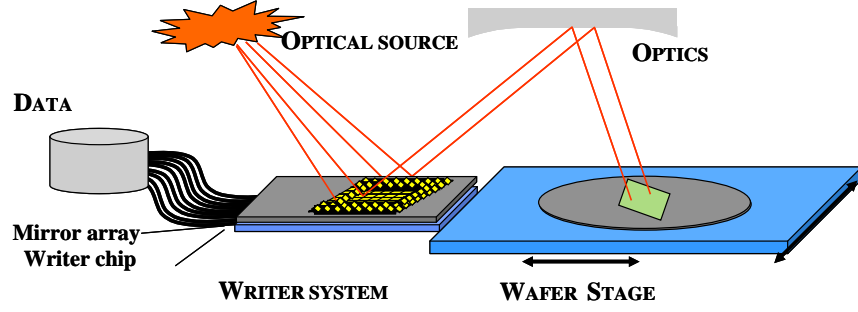


Figure 1.1: Schematic diagram of maskless EUV lithography system [35] [29].

micromirror array, and all mirrors have to be updated after each flash. As a result, we can use only one writer system to create patterns for all layers of layout, and the cost of multiple masks is saved. This is especially beneficial for low-volume application specific integrated circuit (ASIC) designs, since unlike general-purposed processors, the cost of masks can not be averaged out by mass production. On the other hand, the real-time data update, from the storage device to the writer chip, and from the writer chip to the micromirror array, creates the data delivery problem of the direct-write lithography, i.e., making sure all the mirrors can be updated between two flashes. It is obvious that integrating the writer chip and the micromirror array into one chip can solve the second part of the problem, for the interconnection delay within a chip is manageable. However, transmitting the data from the external storage to the writer chip is still an open problem.

### 1.3 Datapath Implementation of Maskless Lithography Systems

To be competitive with today's optical lithography systems, direct-write maskless lithography needs to achieve throughput of one wafer layer per minute. In addition, for 45 nm technology, to achieve the 1 nm edge placement required to comply with the minimum grid size specification as well as the 22 nm pixel size as the design rule scale, a 5-bit per pixel data representation is needed to refine the edge placement precision of pixels to less than 1 nm. Combining these together, the data rate requirement for a maskless lithography system is

$$\frac{(300 \text{ mm})^2}{(22 \text{ nm})^2} \times \frac{\pi}{4} \times \frac{5 \text{ bits}}{60 \text{ s}} = 12 \text{ Tb/s}.$$

To achieve such a data rate, Vito Dai has proposed a data path architecture shown in Figure 1.2 [11]. In this architecture, rasterized, flattened layouts of an integrated circuit (IC) are compressed and stored in a mass storage system. Assuming a 10:1 compression ratio for all layers, the layout of a 22mm  $\times$  22mm chip with 40 layers occupies 20 Tb, as illustrated in Figure 1.2. The compressed layouts are then transferred to the processor board with enough memory to store one layer at a time. This board transfers the compressed layout to the writer chip, composed of a large number of decoders and actual writing elements. The outputs of the decoders correspond to uncompressed layout data and are fed into D/A converters driving the writing elements such as a micromirror array or E-beam writers. In this architecture, the writer system is independent of the data-delivery path, and as such,

the path and the compression algorithm can be applied to arbitrary direct-write lithography systems.

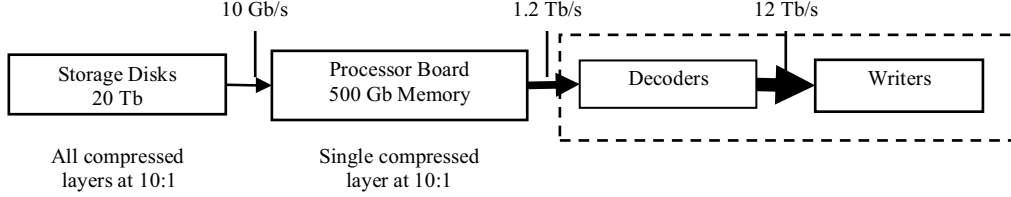


Figure 1.2: Data delivery path of direct-write lithography systems.

In the proposed data-delivery path, compression is needed to minimize the transfer rate between the processor board and the writer chip, and also to minimize the required disk space to store the layout. In Figure 1.2, the total writer data rate of 12 Tb/s is reduced to 1.2 Tb/s assuming compression ratio of 10:1, and then further reduced to 10 Gb/s by using on-board memory with high performance I/O interfaces [4] [31]. Since there are a large number of decoders operating in parallel on the writer chip, an important requirement for any compression algorithm is to have a very low decoder complexity.

Although the 60 wafer layers per hour (WPH) data rate was proposed in [11], in today's proposed direct-write lithography systems, a more conservative 3–7 WPH, or 500 Gb/s data rate is projected to be feasible according to the physical constraints of the optical and electrical sources [33]. Nevertheless, the data rate is still too high for raw data transmission. As a result, lossless compression algorithms are still essential to solve the data-delivery problem of the writer systems, with the same low complexity requirement for the decoder.

To this end, we have proposed a spectrum of lossless layout compression algorithms for

flattened, rasterized data within the family of context-copy-combinatorial-code (C4), which have been shown to outperform all existing techniques such as BZIP2, 2D-LZ, and LZ77 in terms of compression efficiency, especially under limited decoder buffer size, as required for hardware implementation. However, the results shown in [27] and [10] only proved the simplicity of the software decoding. The remaining question is: can those lossless compression algorithms be implemented in hardware and ultimately be integrated into the writer chip with a minimal amount of overhead? This is the main question I answer in this thesis.

## 1.4 Related Work on Maskless Lithography

Although the research on direct-write maskless lithography has been on going for a decade, the main research focus is still on developing a prototype system. Table 1.1 lists a sample of on going electron-beam maskless lithography projects in Europe and United States [34] [33]. The schematics of MAPPER, projection maskless lithography (PML2), and Vistec systems are shown in Figures 1.3, 1.4, and 1.5 respectively. Although these three systems have different energy levels, current densities, and beam splitting mechanisms, they all adapt the architecture from scanning electron microscope (SEM), where the electron gun is placed on top, followed by patterning mechanism, condenser lens, and wafer. On the other hand, reflective E-beam lithography (REBL) places the patterning device, i.e., digital pattern generator (DPG) on the side, and bends the E-beam using a magnetic field, as shown in Figure 1.6. In spite of the differences among the system architectures, the patterning devices in these systems have to be updated dynamically to create layout patterns for different por-

tions of the wafer. As a result, the data delivery issue is a common problem throughout these systems, especially while updating the patterning device for the targeted numbers of beams at a realistic rate, as shown in Table 1.1. Among them, pre-alpha MAPPER system has been delivered to customers, and REBL is scheduled to be delivered by 2012. However, these prototype systems can only create simple patterns with low throughput, for proof of concept purposes. None of the systems achieves realistic throughput for mass production, and the data path to the patterning devices for realistic throughput has not been fully investigated yet.

Table 1.1: List of E-beam direct-write lithography projects [34].

System	MAPPER [24]	PML2 [25]	Vistec [36]	REBL [33]
E-Beam energy	5 keV	50 keV	50 keV	5 keV
Current density	0.3 nA/sub-beam	2 A/cm <sup>2</sup>	5 A/cm <sup>2</sup>	11 $\mu$ A/beam
Patterning device	Beam blanker array	Aperture plate system (APS)	Multi deflection arrays	Digital pattern generator (DPG)
Targeted # of beams	13,000	500,000	64	65536

Besides E-beam approach, EUV maskless lithography has been developed using micromirror array approach in UC Berkeley [35], although the array has not been scaled to the required data throughput. Such a micromirror array approach can also be found in [38] by ASML, along with the proximity correction algorithms. For both E-beam and optical source approaches, the source needs to be charged to reach the required energy level or current density, resulting in the 3–7 WPH constraint.

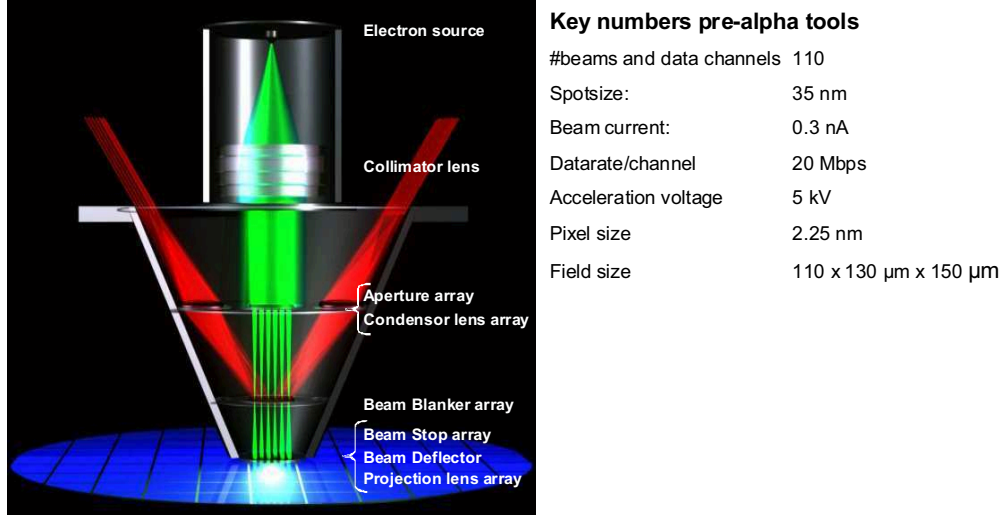


Figure 1.3: Block diagram of pre-alpha MAPPER maskless lithography system [24].

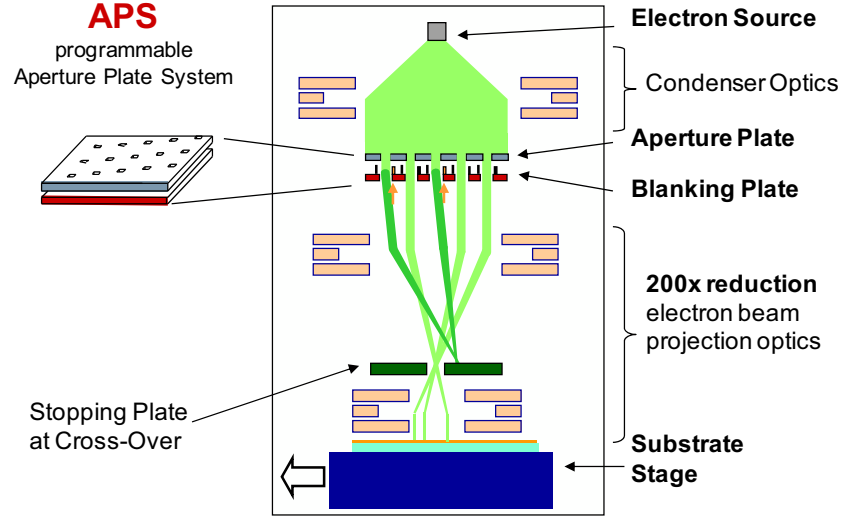


Figure 1.4: Block diagram of PML2 system [34] [25].

Regarding data delivery issue, both electronic links and optical links have been considered as data transfer interface [31] [25]. However, the existing approaches do not scale to the required data throughput, and compression should be applied to balance the difference. In addition, a mixed-signal circuit has been presented to convert pixel values to control

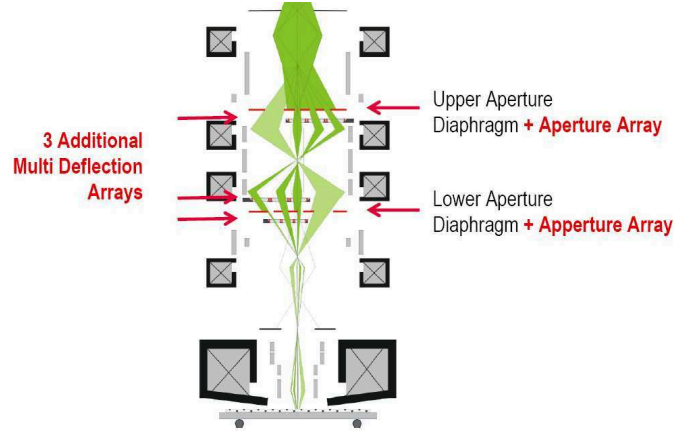


Figure 1.5: Block diagram of Vistec system showing the combination of single shaped beam path (light green) and multi shaped beam path (dark green) [34] [36].

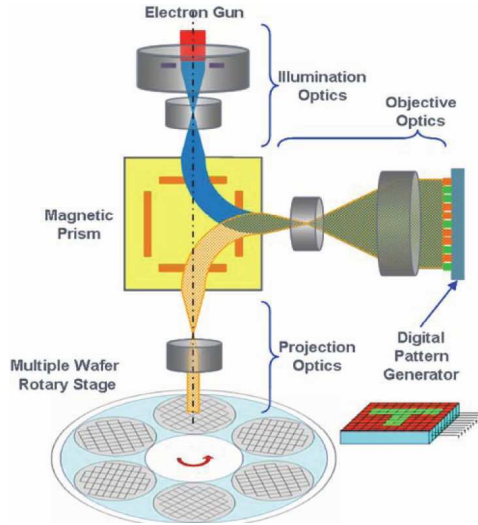


Figure 1.6: Block diagram of REBL system [33].

voltages [40] [16], while a LZ-77 decoder has been implemented to prove the feasibility of integrating data compression into the data path [42].



## 1.5 Scope of the Dissertation

The scope of this dissertation is as follows: in Chapter 2, the prior work on lossless data compression algorithms is presented, including the overview of C4, the original compression algorithm for rasterized, flattened, gray-level layout images, and Block C4, an improved variation of C4 in terms of complexity reduction. Using Block C4 as the starting point, we investigate the hardware implementation of the decompression algorithms.

However, before we start designing the decoder in digital circuits, we have to further simplify the compression algorithms for implementation purposes. As a result, in Chapter 3 we introduce Block Golomb Context-Copy Code (GC3), a variation of Block C4 which results in a simple and fast decoder architecture. Along with Block C4, some other strategies are presented to reduce the decoder complexity.

Chapter 4 shows the hardware implementation of the decoder, with the algorithm converted to data-flow architecture. Inside the decoder, each functional block is discussed in detail, with the schematics presented. At the end of the chapter, the FPGA and ASIC synthesis results of the Block GC3 decoder are presented, showing the applicability of integrating the decoder into the writer chip of direct-write lithography systems.

In Chapter 5, we discuss other hardware implementation issues for the writer system data path, including on-chip input/output buffering, error propagation control, and input data stream packaging. This hardware data path implementation is independent of the writer systems or data link types, and can be integrated with arbitrary direct-write lithography systems.

In Chapter 6, we use reflective electron-beam lithography (REBL) system as an example to study the performance of Block GC3. In this system, the layout patterns are written on a rotary writing stage, resulting in layout data which is rotated at arbitrary angles with respect to the pixel grid. Moreover, the data is subjected to E-beam proximity correction effects. Applying the Block GC3 algorithm to E-beam proximity corrected and rotated layout data can result in poor compression efficiency far below those obtained on Manhattan geometry and without E-beam proximity correction. Consequently, Block GC3 needs to be modified to accommodate the characteristics of REBL data while maintaining a low-complexity decoder for the hardware implementation. In this chapter, we modify Block GC3 in a number of ways in order to make it applicable to the REBL system; we refer to this new algorithm as Block Rotated Golomb Context Copy Coding (Block RGC3). The modifications and the corresponding encoder complexity issues are discussed in this chapter.

Chapter 7 presents the summary of this work and a forward to some possible future research topics toward lossless data compression and direct-write lithography.

## Chapter 2

### Prior Work on Lossless Data

### Compression Algorithms for Maskless Lithography Systems

In the proposed data-delivery path in Chapter 1, compression is needed to minimize the transfer rate between the processor board and the writer chip, and also to minimize the required disk space to store the layout data. Since there are a large number of decoders operating in parallel on the writer chip to achieve the projected output data rate, an important requirement for any compression algorithm is to have an extremely low decompression complexity. To this end, Vito Dai and I have proposed a series of lossless layout compression algorithms for flattened, rasterized data [14] [27]. In this chapter, the previous work on lossless layout image compression is reviewed. In particular, the family of Context Copy

Combinatorial Code (C4) compression algorithms are introduced in detail.

## 2.1 Overview of C4

While observing the flattened, layout images, we can notice two prominent characteristics: Manhattan shape of the patterns, and repetitiveness of the patterns, as shown in Figure 2.1. Moreover, layout images consist of only monotone foreground (layout patterns) and background. By denoting foreground pixels as “1”s and background pixels as “0”s, the layout images can be represented in binary level, with the pixel grid equals the edge placement grid. In such a case, bi-level context prediction, e.g., JBIG, can be applied to predict the Manhattan patterns [1] [11]. On the other hand, for the repetitive patterns, a 2-dimensional Lempel-Ziv style copying method was developed to achieve compression efficiency [48] [9]. However, if we consider the pixel size as the design rule scale, i.e., half of the minimum feature size, and 1 nm edge placement as in GDS file specifications, such a binary image model no longer sustains, and the layout image must be represented in gray scale by applying rasterization [12]. To compress such flattened, rasterized gray-level layout images, new lossless image compression algorithm is needed.

To compress the images efficiently, we must utilize both characteristics by either predicting the pixel value from its neighborhood to preserve the horizontal and vertical edges of the patterns, or copying the patterns directly from the buffer to exploit the repetition of the data. The family of Context Copy Combinatorial Code (C4) compression algorithms combines those two techniques, local context-based prediction [41] and Lempel-Ziv (LZ)

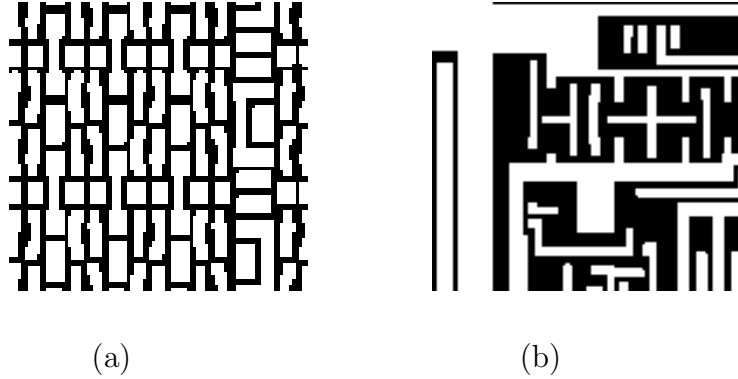


Figure 2.1: (a)Repetitive and (b) non-repetitive layouts.

style copying, to achieve lossless compression for the rasterized layout images. In other words, the encoder divides the layout images into “predict” and “copy” regions, which are non-overlapping rectangles, and only the residues from the prediction and copy operations are transmitted to the decoder. By avoiding redundant transmission of copied or predicted pixels, C4 achieves high compression efficiency.

Figure 2.2 shows a high-level block diagram of the C4 encoder and decoder for flattened, rasterized gray-level layout images. First, a prediction error image is generated from the layout, using a simple three-pixel prediction model to be described shortly. Next, the “Find copy regions” block uses the error image to segment the layout image automatically, i.e., generate a segmentation map between copy and predict regions. As specified by the segmentation, the predict/copy block estimates each pixel value, either by copying or by prediction. The result is compared to the actual value in the layout image. Correct pixel values are indicated with a “0” and incorrect values are indicated with a “1.” The pixel error location is compressed without loss by the hierarchical combinatorial code (HCC) encoder [13] [14], and

the corresponding pixel error value is compressed by the Huffman encoder. These compressed bit streams are transmitted to the decoder, along with the segmentation map, indicating the copy and predict regions of the layout images.

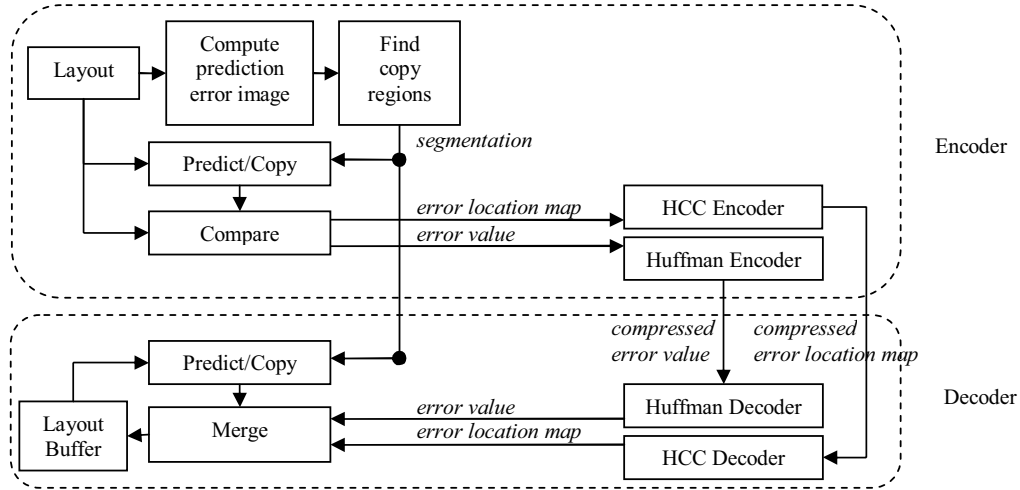


Figure 2.2: Block diagram of C4 encoder and decoder for gray-level images.

The decoder mirrors the encoder, but skips the complex process necessary to find the segmentation map, which is directly received from the encoder. The HCC decoder decompresses the error location bits from the encoder. As specified by the segmentation, the Predict/Copy block estimates each pixel value, either by copying or by prediction. If the error location bit is “0”, the pixel value is correct, and if the error location bit is “1”, the pixel value is incorrect, and must be replaced by the actual pixel value decoded from Huffman decoder. There is no segmentation performed in the C4 decoder, so it is considerably simpler to implement than the encoder.

Linear prediction is used in C4, where each pixel is predicted from its three-pixel neigh-

borhood as shown in Figure 2.3. Pixel  $z$  is predicted as a linear combination of its local 3-pixel neighborhood  $a$ ,  $b$ , and  $c$ . If the prediction value is negative or exceeds the maximum allowed pixel value  $max$ , the result is clipped to 0 or  $max$  respectively. The intuition behind this predictor is simple: pixel  $b$  is related to pixel  $a$ , the same way pixel  $z$  relates to pixel  $c$ . For example, in a region of constant intensity, i.e.,  $a = b = c$ , then predicting  $z = c$  continues that region of constant intensity. On other hand, if there is a vertical edge, i.e.,  $a = c$ , then the algorithm will predict  $z = b + c - a = b$ , resulting in a continuation of the vertical edge. Likewise, if there is horizontal edge, the algorithm will predict the current pixel being  $z = b + c - b = c$ , and the horizontal edge is preserved. Thus, these equations predict continuations of horizontal edges, vertical edges, and regions of constant intensity. Interestingly, this linear predictor can also be applied to a binary image by setting  $max = 1$ , resulting in the same predicted values as binary context-based prediction proposed in the binary C4 [14]. It is also similar to the median predictor used in JPEG-LS [41]. The linear prediction is used in both encoder and decoder, as shown in Figure 2.2.

This prediction mechanism typically fails only at corners of polygons, so the number of prediction error pixels is proportional to the number of polygon vertices. Therefore, for sparse features, it is advantageous to apply predictions, as empirically verified in [10]. On the other hand, for dense or repetitive layouts, if the encoder can automatically find the repetition within the image and code it appropriately, the copy error pixels, i.e., the pixels which can not be copied, will dramatically be reduced. The compression efficiency is directly related to the numbers of image error pixels, which is the total number of prediction error

pixels and copy error pixels. In C4, the major task is to develop an automatic algorithm to minimize the number of image error pixels.

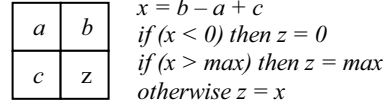


Figure 2.3: Three-pixel linear prediction with saturation in C4.

It is obvious that the segmentation operation in the C4 encoder is extremely computationally intensive, and is vital to the compression efficiency of C4. In fact, a greedy heuristics search algorithm is applied in C4, resulting in the best compression efficiency as compared to all existed lossless compression algorithms [14]; however, the encoding time of C4 is also larger than other algorithms. To reduce this computational overhead, a variant of C4, called Block C4, is developed.

## 2.2 Block C4

In C4, the segmentation is described as a list of rectangular copy regions. An example of a copy region is shown in Figure 2.4. Each copy region is a rectangle, enclosing a repetitive section of a layout, described by 6 attributes: the rectangle position  $(x, y)$ , its width and height  $(w, h)$ , the orthogonal direction of the copy ( $dir = left$  or  $above$ ), and the distance to copy from  $(d)$ , i.e., the period of the repetition.

It is not trivial to find the “best” segmentation automatically. Even in such a simple



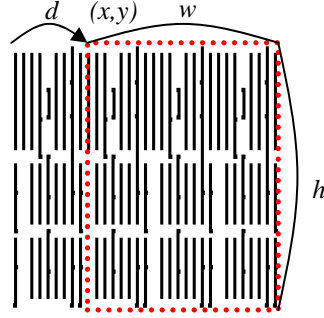


Figure 2.4: Illustration of a copy region.

example shown in Figure 2.4, there are many potential copy regions, a few of which are illustrated in Figure 2.5 as dotted and dashed rectangles. The number of all possible copy regions is of the order of  $O(N^5)$  for  $N \times N$  pixel layout, and choosing the best set of copy regions for a given layout is a combinatorial problem. Exhaustive search in this space is prohibitively complex, and C4 already adopts a number of greedy heuristics to make the problem tractable. Nevertheless, further complexity reduction of the segmentation algorithm is desirable.

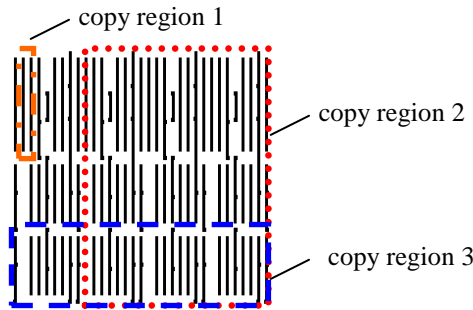


Figure 2.5: Illustration of a few potential copy regions that may be defined on the same layout.

Block C4 adopts a far more restrictive segmentation algorithm than C4, and as such, is much faster to compute. Specifically, Block C4 restricts both the position and sizes to fixed  $M \times M$  blocks on a grid whereas C4 allows for copy regions to be placed in arbitrary  $(x, y)$  positions with arbitrary  $(w, h)$  sizes. Figure 2.6 illustrates the difference between Block C4 and C4 segmentations. In Figure 2.6(a), the segmentation for C4 is composed of 3 rectangular copy regions, with 6 attributes  $(x, y, w, h, dir, d)$  describing each copy region. In Figure 2.6(b), the segmentation for Block C4 is composed of twenty  $M \times M$  tiles, with each tile marked as either prediction ( $P$ ), or copy with direction and distance  $(dir, d)$ . This simple change reduces the number of possible copy regions to

$$O\left(\frac{N^3}{M^2}\right) \approx \frac{N^2}{M^2} \times O(N),$$

a substantial  $N^2M^2$  reduction in search space compared to C4. For our test data,  $N = 1024$  and  $M = 8$ , so the copy region search space has been reduced by a factor of 64 million. However, this complexity reduction could potentially come at the expense of compression efficiency, as illustrated in Section 2.3.

The complexity reduction is also a function of the block size  $M$ , where the smaller the block size, the better approximation of Figure 2.6(a) by Figure 2.6(b). In this case, Block C4 and C4 result in the same segmentation map, hence the same number of image errors. However, in this scenario, the segmentation map of Block C4 is broken down to too many tiles, and transmitting the segmentation information becomes a challenge for the encoder. To balance these two effects, We have empirically found  $M = 8$  to exhibit the best compression efficiency for nearly all test cases as compared to  $M = 4$  or  $M = 16$ .

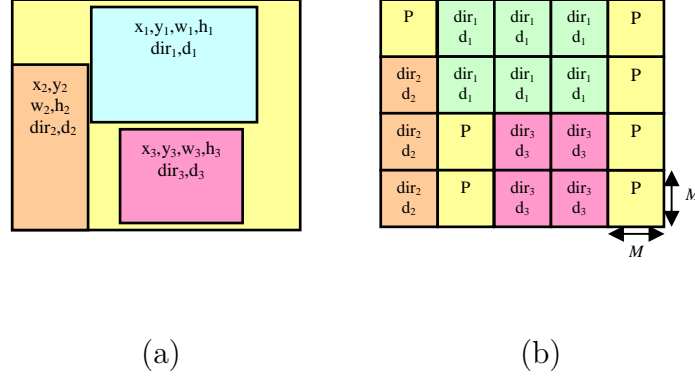


Figure 2.6: Segmentation map of (a) C4 vs. (b) Block C4.

To further improve the compression efficiency of Block C4, we note that the segmentation shown in Figure 2.6(b) is highly structured. Indeed, the segmentation can be used to represent boundaries in a layout separating repetitive regions from non-repetitive regions, and that these repetitions are caused by design cell hierarchies, which are placed on an orthogonal grid. Consequently, Block C4 segmentation has an orthogonal structure, and C4 already employs a reasonably efficient method for compressing orthogonal structures placed on a grid, namely context-based prediction.

To encode the segmentation, blocks are treated as pixels, and the attributes  $(P, dir, d)$  as colors of each block. Each block is predicted from its three-block neighborhood, as shown in Figure 2.7. For vertical edges corresponding to  $c = a$ ,  $z$  is likely to be equal to  $b$ . Similarly for horizontal edges corresponding to  $a = b$ ,  $z$  is likely to be equal to  $c$ . Consequently, the prediction shown in Figure 2.7 only fails around corner blocks, which are assumed to occur less frequently than horizontal or vertical edges. Applying context-based block prediction to the segmentation in Figure 2.8(a), we obtain Figure 2.8(b) where  $\checkmark$  marks indicate correct

predictions. The pattern of marks could be compressed using HCC or any other binary coding techniques, and the remaining values of  $(P, dir, d)$  could be Huffman coded, exactly analogous to the method of coding copy/prediction error bits and values used in C4. For Block C4, we choose to use Golomb run-length coder to compress segmentation error locations. This is because the segmentation error location amounts to a very small percentage of the output bit stream, and as such, applying a complex scheme such as HCC is hard to justify.

$a$	$b$
$c$	$z$

$$\begin{array}{l} \text{If } (c = a) \text{ then } z = b \\ \text{else } z = c \end{array}$$

Figure 2.7: Three-block prediction for encoding segmentation in Block C4.

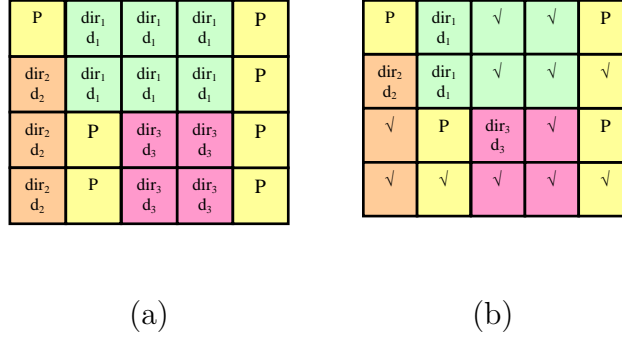


Figure 2.8: (a) Block C4 segmentation map (b) with context-based prediction.

## 2.3 Compression Efficiency Results

The full table of results, comparing Block C4 to C4 is shown in Table 2.1 [10]. In it, we compare the compression efficiency and encoding time of various  $1024 \times 1024$  5-bit gray-scale images, generated from different sections and layers of an industry microchip. In columns, from left to right, are the layer image name, C4 compression ratio, C4 encode time, Block C4 compression ratio, and Block C4 encode time. Both C4 and Block C4 use the smallest 1.7 KB buffer, corresponding to only 2 stored rows of data. Encoding times are generated on an AMD Athlon64TM 3200+ Windows XP desktop with 1 GB of memory.

A quick glance at this table makes it clear that the speed advantage of Block C4 over C4 is universal, i.e., over 100 times faster than C4, and consistent, i.e., 13.7 to 14.1 seconds, for all layers and layout types tested. In general, the compression efficiency of Block C4 matches that of C4. One exception is row 5 of Table 2.1, where C4 exceeds the compression efficiency of Block C4, on the highly regular M1-memory layout.

For this layout, C4's compression ratio is 13.1, while Block C4's compression ratio is 9.5. In this particular case, the layout is extremely repetitive, and C4 covers 99% of the entire  $1024 \times 1024$  image with only 132 copy regions. Moreover, many of these copy regions are long narrow strips, less than 8-pixels wide, which Block C4 cannot possibly duplicate. Consequently, Block C4 exhibits a loss of compression efficiency as compared to C4, in this particular case. Reducing the block size of Block C4 may potentially improve the compression efficiency, since C4 can be treated as a special case of Block C4 with the block size of  $1 \times 1$ .

The other comparison is performed among, C4, Block C4, and other existing lossless

Table 2.1: Comparison of compression ratio and encode times of C4 vs. Block C4 [10].

Layout	C4		Block C4	
	Compression ratio	Encoding time	Compression ratio	Encoding time
Poly-memory	7.60	1608 s	7.63	14.0 s
		(26.8 min)		(115 $\times$ speedup)
Poly-control	9.18	12113 s	9.18	13.9 s
		(3.4 hr)		(865 $\times$ speedup)
Poly-mixed	10.6	1523 s	11.35	13.9 s
		(25.4 min)		(110 $\times$ speedup)
M1-memory	13.1	3841 s	9.50	13.9 s
		(1.1 hr)		(276 $\times$ speedup)
M1-control	18.7	13045 s	17.3	13.9 s
		(3.6 hr)		(938 $\times$ speedup)
M1-mixed	15.5	13902 s	14.7	13.9 s
		(3.9 hr)		(1000 $\times$ speedup)
Via-dense	10.2	3350 s	15.5	14.1 s
		(55.8 min)		(237 $\times$ speedup)
Via-sparse	16.0	7478 s	21.6	13.7 s
		(2.1 hr)		(546 $\times$ speedup)

compression algorithms, including Huffman, ZIP, BZIP2, run-length code, and LZ77 [22] [2] [48]. Figure 2.9 shows the compression efficiency of these algorithms over different decoder

buffer sizes [10]. The data points in the plot denote the lowest compression ratio in our test images using the specific decoder buffer size. It is obvious that Block C4 and C4 outperform all the existing lossless compression algorithms. BZIP2, in this plot, achieves similar compression efficiencies as compared to Block C4; however, the decoder buffer size required by BZIP2 is three orders of magnitude greater than Block C4, and its algorithm is impractical to be implemented in hardware.

By using 1.7 KB of decoder buffer, Block C4 can successfully satisfy the compression efficiency requirement for the data path of direct-write lithography systems. The remaining question is: Can this algorithm be implemented in hardware with the minimum cost in terms of the area and power? This is the question we are going to address in the remaining part of the thesis.

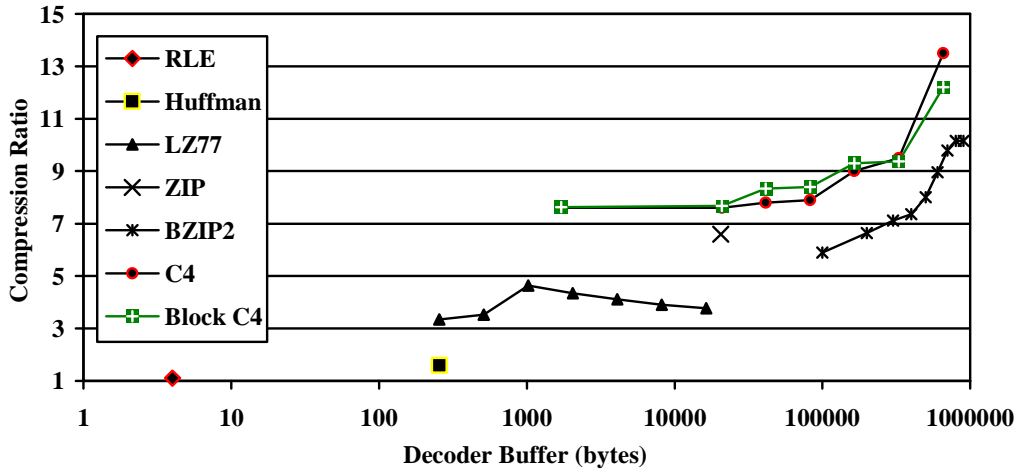


Figure 2.9: The compression efficiency comparison among different lossless compression algorithms [10].

## Chapter 3

# Block GC3 Lossless Compression

## Algorithm

### 3.1 Introduction

Before we start designing the decoder in digital circuits, we have to further simplify the compression algorithms for implementation purposes. Specifically, we have to reduce the number of data streams, and ensure parallelism of the decoding architecture. In software decoding, since the instructions are executed sequentially, results from the previous functions are naturally ready for the current operation. However, in hardware, such sequential operation is controlled by a state machine, and often results in a low throughput or a complicated design. In this chapter, we modify Block C4 algorithmically to avoid sequential decoding, along with some other optimization strategies. The resulting algorithm, Block



Golomb Context-Copy Code (GC3), is discussed in detail in the remainder of the chapter.

## 3.2 Block GC3

In both C4 and Block C4, the error location bits are compressed using HCC. While HCC is useful for encoding the highly-skewed binary data in a lossless fashion [13], when it comes down to hardware implementation, the hierarchical structure of HCC implies repetitive hardware blocks and inevitable decoding latency from the top level to the final output. Moreover, as we show in Chapter 4, the HCC block becomes the bottleneck of the entire system due to its long delay. To overcome this problem, we propose to replace HCC in Block C4 by a Golomb run-length coder [17], resulting in a new compression algorithm called Block Golomb Context Copy Code (Block GC3). As such, Golomb run-length coder in Block GC3 is now used to encode error locations of both the pixels in the layout and the segmentation blocks in the segmentation map. Figure 3.1 shows the block diagram for Block GC3, which is more or less identical to that of C4 shown in Chapter 2 with the exception of the pixel error location encoding scheme and segmentation map compression as discussed in Chapter 2

Coding the pixel error location of layouts with Golomb run-length code could potentially lower the compression efficiency. Figure 3.2 shows a binary stream coded with both HCC and Golomb run-length coder. In the upper path, the stream is coded with Golomb run-length coder. In this case, the input stream is either coded as  $(0)$ , denoting a stream of  $B$  zeroes, where  $B$  denotes a predefined bucket size, or coded as  $(1, n)$ , indicating a “1” occurs after  $n$  zeroes. In general, the Golomb code requires integer multiplication and division. To simplify

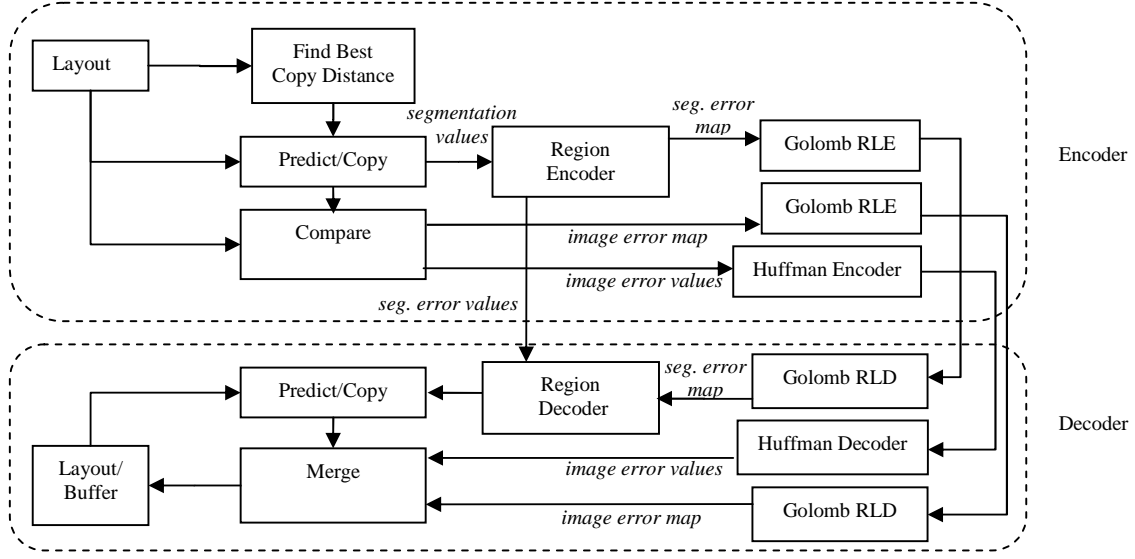


Figure 3.1: The encoder/decoder architecture of Block GC3.

it to bit-shifting operation, we restrict  $B$  to be power of 2. These parameters are further converted into a bit stream, where parameter (0) is translated into a 1-bit codeword, and  $(1, n)$  takes  $1 + \log_2 B$  bits to encode. Therefore, a stream with successive ones can potentially be encoded into a longer code than a stream with ones which are far apart from each other. On the other hand, in the lower path of Figure 3.2, HCC counts the number of ones within a fixed block size and codes it using enumerative code [14]. In Figure 3.2, the block size is 8 and attributes  $(2, 11)$  denote the 11<sup>th</sup> greatest 8-bit sequence with two “1”s, i.e., “01000010.” The attributes  $(2, 11)$  are further translated to codewords “010” and “01011,” which are the binary representations of 2 and 11 respectively. As long as the number of ones inside the block is fixed, HCC results in a fixed length bit stream regardless of the input distribution.

Based on the above, Block GC3 can result in potential compression efficiency loss for

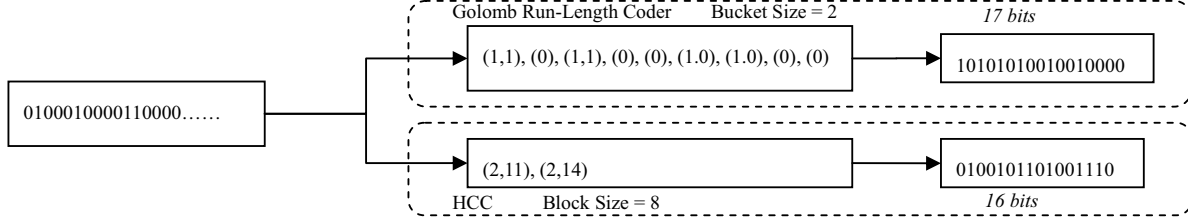


Figure 3.2: Golomb run-length encoding process.

certain class of images. Specifically, Figure 3.3 shows a typical layout with successive prediction errors occurring at the corner of Manhattan shapes due to the linear prediction property. Since error locations are not distributed in an independent-identically distributed (i.i.d.) fashion, there is potential compression efficiency loss due to Golomb run-length coder as compared to HCC. To alleviate this problem, we adapt the bucket size for Golomb run-length coder from layer to layer.

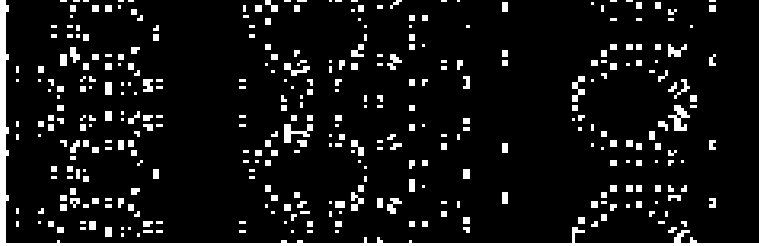


Figure 3.3: Visualization of pixel error location for a layout image.

As shown in Table 3.1, Block GC3 results in about 10 to 15 % lower compression efficiency than Block C4 over different process layers of layouts assuming decoder buffer size of 1.7 KB. The test images in Table 3.1 are  $1024 \times 1024$  5-bit grayscale rasterized, flattened layouts, examples of which are shown in Figures 3.3. Similarly, Figure 3.4 compares the minimum

Table 3.1: Compression efficiency comparison between Block C4 and Block GC3 for different layers of layouts.

Layers	Compression ratio	Compression ratio	Bucket size for
	(Block C4)	(Block GC3)	Block GC3
Metal 1 control	16.84	14.74	32
Metal 1 memory	9.33	8.37	16
Metal 1 mixed	14.21	12.67	16
Metal 2 mixed	33.81	28.83	64
$N$ active mixed	43.10	36.51	64
$P$ active mixed	66.17	59.24	128
Poly control	8.96	7.80	8
Poly memory	7.47	6.51	8
Poly mixed	11.00	9.633	16

compression efficiency of Block C4, Block GC3, and few other existing lossless compression schemes as a function of decoder buffer size [10]. The minimum is computed over ten  $1024 \times 1024$  images manually selected among five layers of two IC layouts. In practice, we focus on 1.7 KB buffer size for hardware implementation purposes. While Block GC3 results in slightly lower compression efficiency than Block C4 for nearly all decoder buffer sizes, it outperforms all other existing lossless compression schemes such as LZ77, ZIP [48], BZIP2 [2], Huffman [22], and run-length encoder (RLE).

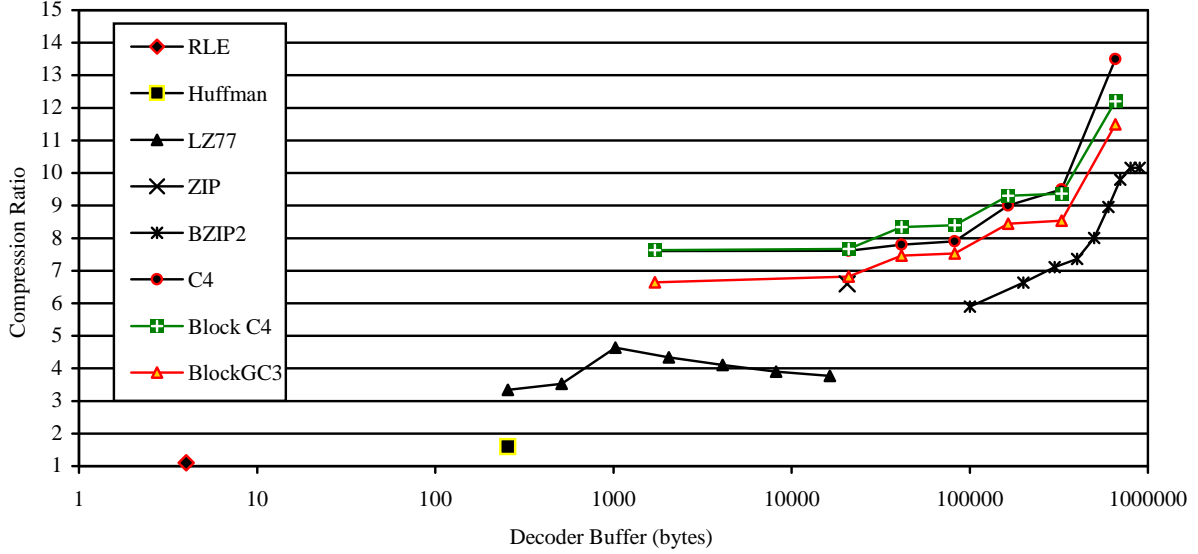
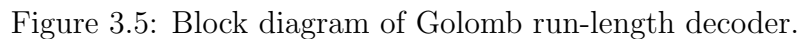


Figure 3.4: Compression efficiency and buffer size tradeoff for Block C4 and Block GC3.

### 3.3 Selectable Bucket Size for Golomb Run-Length Decoder

In the previous section, we discussed the simplicity of Golomb run-length decoding algorithm. Due to varying image error rates of the layout images over different layers, the bucket size  $B$  of the Golomb run-length decoder needs to be tuned from image to image in order to achieve the best compression efficiency. In terms of hardware design, this implies the width of the data bus has to match  $\log_2 B_{max}$ , where  $B_{max}$  is the greatest bucket size, even though  $B_{max}$  may hardly ever be used. Figure 3.5 shows the block diagram of the Golomb run-length decoder, which reads in the compressed binary Golomb code through a barrel shifter and generates the decompressed binary stream of error locations using the counter



Such a design choice adversely affects the compression efficiency by lowering its upper bound. For example, the compression ratio for a black image goes from 1280 to 316.8, and other easily compressible images will also suffer from lower compression efficiencies. However, those images are not bottleneck of the data path; based on the compression ratio distribution reported in [47], changing the compression efficiency of those images does not significantly affect the overall compression performance of Block GC3. On the other hand, by limiting the bucket size of the Golomb run-length decoder, the hardware resources can be saved, and the routing complexity of the extremely wide data buses can be reduced.

### 3.4 Fixed Codeword for Huffman Decoder

Similar to other entropy codes, Huffman code adapts its codeword according to the statistics of the input data stream to achieve the highest compression efficiency. In general, the codeword is either derived from the input data itself, or by the training data with the same statistics. In both scenarios, the code table in the Huffman decoder has to be updated to reflect the statistical change of the input data stream. For layout images, this corresponds to either different layers or different parts of the layout. However, the updating of the code table requires an additional data stream to be transmitted from encoder to the decoder. Moreover, the update of the code table has to be done in the background such that the current decoding is not affected. Consequently, more internal buffers are introduced, and additional data is transmitted over the data path.

Close examination of the statistics of input data stream, namely, the image error values explained in Chapter 2, reveals that the update can be avoided. Figure 3.6 shows two layout images with their image error value histograms and a selected numbers of Huffman codewords. The left side shows a poly layer and the right one an n-active layer. Although the layout images seem different, the histograms are somewhat similar, and so are the codewords. More specifically, the lengths of the codewords for the same error value are almost identical, except for those on the boundaries and those with low probability of occurrence. The similarity can be explained by the way we generate the error values: After copy and predict techniques are applied, the error pixels are mainly located at the edges of the features. As a result, the error values for different images are likely to have similar probability

Table 3.2: Compression efficiency comparison between different Huffman code tables.

Layout image	Compression ratio		Efficiency loss (%)
	Adaptive Huffman code table	Fixed Huffman code table	
Metal 1	13.06	12.97	0.70
Metal 2	29.81	29.59	0.74
$N$ active	38.12	38.01	0.28
Poly	9.89	9.87	0.17

distributions, even though the total number of error values varies from image to image. Based on this observation, we can use a fixed Huffman codeword to compress all the images without losing too much compression efficiency, in exchange for no code table updating for the decoder. Table 3.2 shows the comparison of the compression efficiency between the fixed Huffman code table and adaptive Huffman code table over several  $1024 \times 1024$  5-bit gray-level images. The compression loss of the fixed code table is less than 1%, and is lower for the low compression ratio images. Therefore, in hardware implementation, we opt to use a fixed Huffman code table to compress all the layout images.

### 3.5 Summary

To implement the lossless compression decoding algorithm in hardware, we modify the original Block C4 algorithm to improve the decoder efficiency. The resulting Block GC3 has a compression efficiency loss of 10–15% as compared to Block C4. However, as we are going



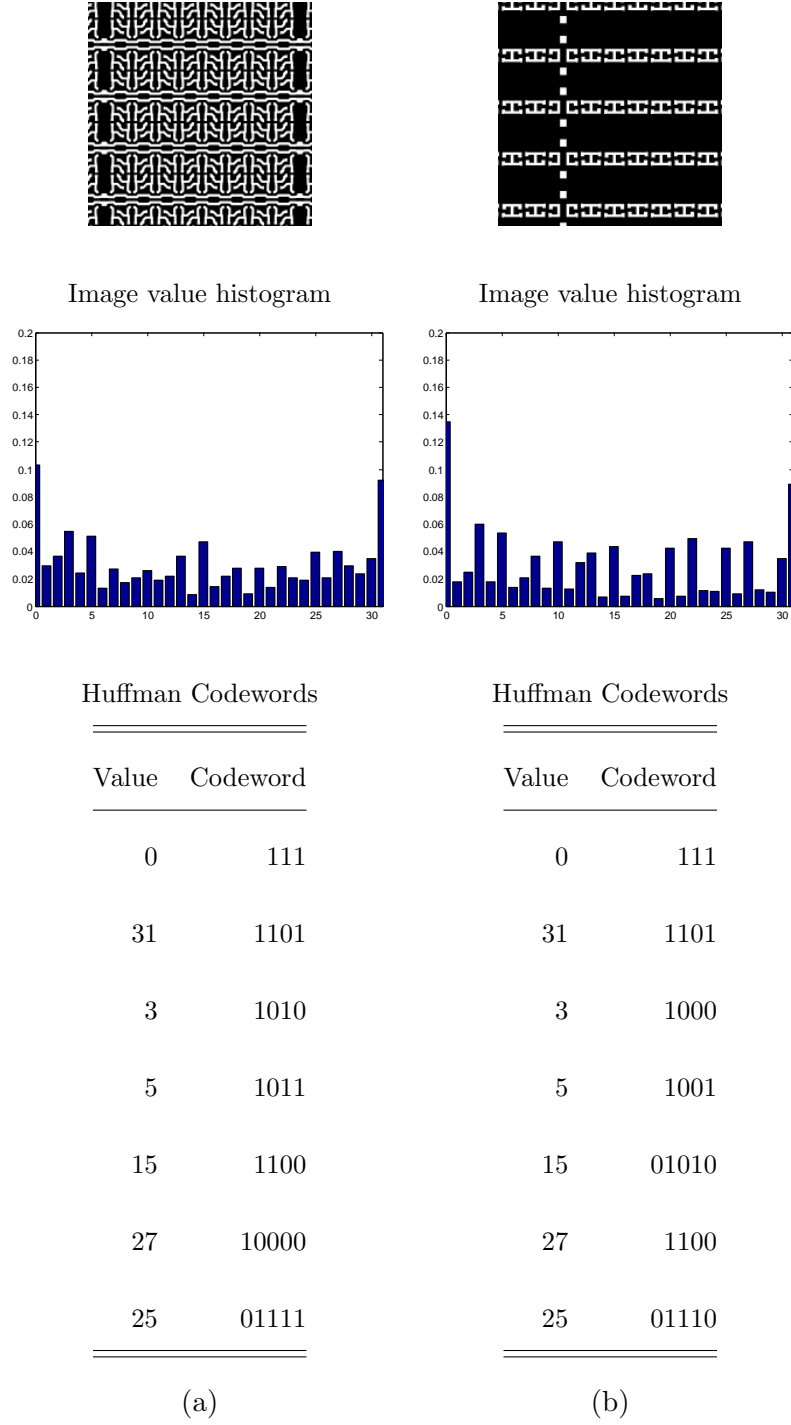


Figure 3.6: Image error value and Huffman codewords comparison, for (a) poly layer and (b) n-active layer.

to show in the next chapter, the decoder design of Block GC3 is much simpler than that of Block C4, thus compensating the compression efficiency loss.

In addition, we restrain the parameter selection for Block GC3, such as defining the maximum bucket size for Golomb run-length code, and using a fixed Huffman code table for image error value coding. As a result, the data bus in the decoder is utilized more, and the input data transmission overhead is reduced.

With these modifications, the lossless decompression algorithm is ready to be implemented in hardware. In the next chapter, we are going to describe the implementation in detail.

## Chapter 4

# Hardware Design of Block C4 and Block GC3 Decoders

### 4.1 Introduction

For the decoder to be used in a maskless lithography data path, it must be implemented as a custom-designed digital circuit and included on the same chip with the writer array. In addition, to achieve a system with high level of parallelism, the decoder must have data-flow architecture and high throughput. By analyzing the functional blocks of the Block C4 and Block GC3 algorithms, we devise the data-flow architecture for the decoder. The block diagram of Block C4 decoder is shown in Figure 4.1. There are three main inputs: the segmentation, the compressed error location, and the compressed error value. The segmentation is fed into the Region Decoder, generating a segmentation map as needed by the decoding

process. Using this map, the decoded predict/copy property of each pixel can be used to select between the predicted value from Linear Prediction and the copied value from History Buffer in the Control/Merge stage, as shown in Figure 4.2. The compressed pixel error location is decoded by HCC, resulting in an error location map, which indicates the locations of invalid predict/copy pixels. In the decoder, this map contributes to another control signal in the Control/Merge stage to select the final output pixel value from either predict/copy value or the decompressed error value generated by Huffman decoder. The output data is written back to History Buffer for future usage, either for linear prediction or for copying, where the appropriate access position in the buffer is generated by Address Generator. All the decoding operations are combinations of basic logic and arithmetic operations, such as selection, addition, and subtraction. By applying the tradeoffs described in Chapter 3, the total amount of needed memory inside a single Block C4 decoder is about 1.7 KB, which can be implemented using on-chip SRAM.

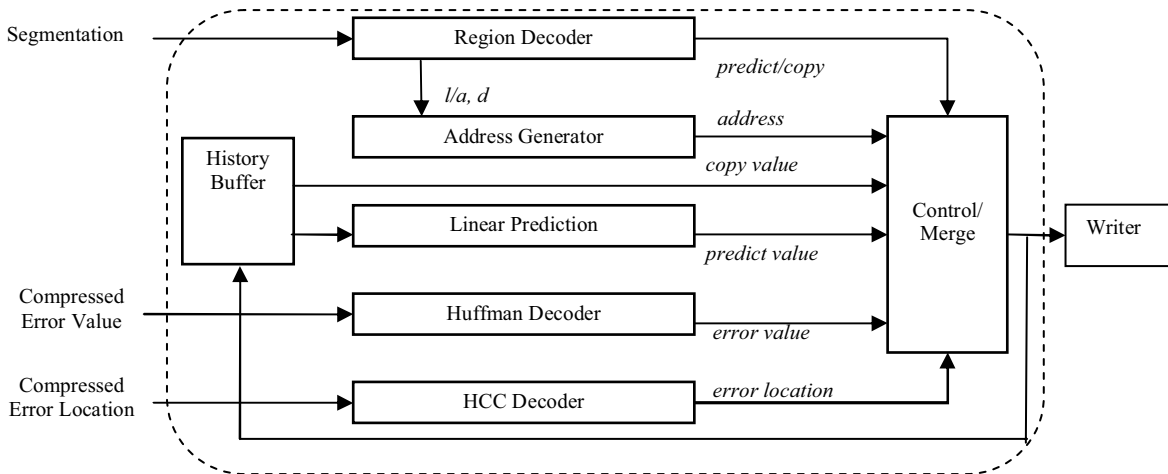


Figure 4.1: Functional block diagram of the decoder.

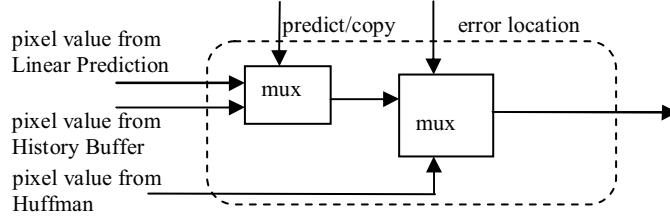


Figure 4.2: The block diagram of Merge/Control block.

The block diagram of Block GC3 is almost identical to that of Block C4 shown in Figure 4.1, since it only replaces the HCC block of Block C4 by a Golomb run-length decoder.

In the remainder of this chapter, we discuss the architecture for the Block C4 and Block GC3 decoders. We will break down all seven major blocks and describe the function in detail. The Simulink schematics of the blocks will be shown in Appendix B. We also present the FPGA and ASIC implementation and synthesis results of Block GC3 decoder.

## 4.2 Block C4

In this section, we examine the functional blocks inside Block C4 decoder and discuss the implementation and the cost of each block.

### 4.2.1 Linear Predictor

For flattened, rasterized layout images, in order to correctly preserve horizontal and vertical edges, we use a 3-pixel linear prediction model to predict the 5-bit gray level images. The prediction strategy is similar to the binary image context-based prediction in [14]. However,

in this block, we only use arithmetic operations instead of table look-up to predict the image pixel values. Besides the 3-pixel based linear prediction, this block also sets two thresholds of 0 and 31 to detect the overflow from addition and subtraction. The block diagram is shown in Figure 4.3.

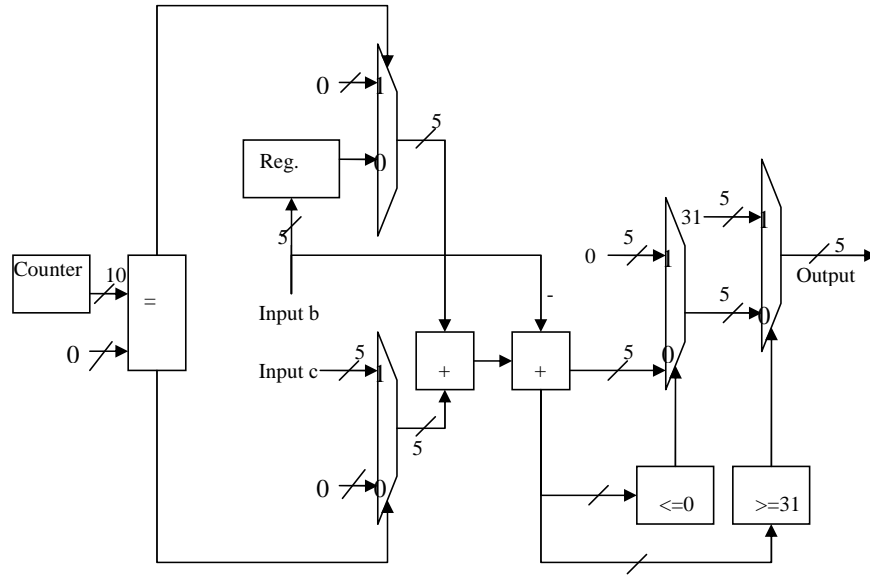


Figure 4.3: The block diagram of Linear Predictor.

$a$	$b$	$x = b - a + c$
$c$	$z$	$\text{if } (x < 0) \text{ then } z = 0$
		$\text{if } (x > \text{max}) \text{ then } z = \text{max}$
		$\text{otherwise } z = x$

Figure 4.4: The algorithm of 3-pixel based linear prediction.

The 3-pixel based linear prediction algorithm is shown in Figure 4.4. Pixel  $z$  is the current pixel we are predicting, and  $a$ ,  $b$ , and  $c$  are three adjacent pixels on the upper, left, and upper-left corner; by applying this simple linear prediction, the horizontal and vertical

edges of the layout images can be preserved, as discussed in Chapter 2. In terms of the implementation of the predictor, we merely have two inputs: pixel  $b$  from the history buffer, and pixel  $c$  the system output from the previous cycle; pixel  $a$  is the delayed version of  $b$ . In addition, we set the upper and left boundaries to 0 in order to provide the initial condition of the linear prediction. Although there are both addition and subtraction in the block, we do not have to use two's complement data representation; since the pixel values are all positive, it is not necessary to spend one extra sign bit to represent the negative values. All we have to do is to check the carry-out output of both adder and subtractor to make sure we handle the overflow cases properly.

## 4.2.2 Region Decoder

### Architecture

In the C4 algorithm, each flattened, rasterized layout image is divided into copy and predict regions; copy distances and directions for copy regions are also annotated so that the decoder can access the history buffer properly. Similar to an actual IC layout, the segmentation map is also Manhattan shaped, and can be compressed by the prediction algorithm. However, since the segmentation map, consisting of the segmentation information (*predict/copy, direction, distance*), is an artificial image, there is no correlation between the information of adjacent regions. Considering the simplicity and the benefit from several prediction algorithms, the segmentation predictor shown in Figure 4.5 is used in the region decoder rather than the linear predictor used for pixel predictions in a layout. The resulting

two bit streams, the segmentation error location and the segmentation error value, are transmitted to the decoder. In particular, the segmentation error location is further compressed using Golomb run-length code.

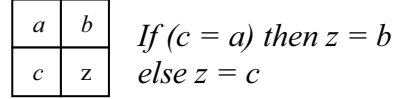


Figure 4.5: The context prediction algorithm for the segmentation information.

In the decoder, the region decoder block restores the segmentation information for each  $8 \times 8$  image microblock from the compressed segmentation error location and the segmentation error value. Furthermore, it has to convert the segmentation information from the  $8 \times 8$  block domain to the pixel domain, since the other operations in the decoder are done pixel by pixel. The architecture of the region decoder is shown in Figure 4.6. The core of the region decoder is the segmentation predictor, and the output of the region decoder is selected to be either the error value or the output of the segmentation predictor, depending on the segmentation error location provided by the Golomb run-length decoder.

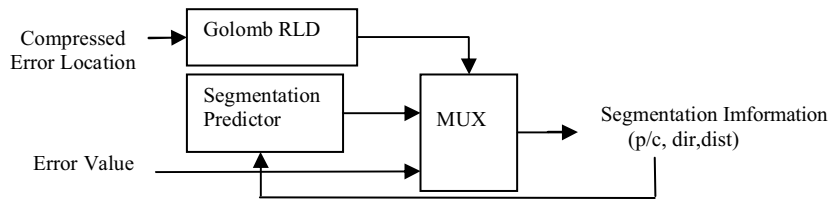


Figure 4.6: The block diagram of the region decoder.

This region decoder has several architectural advantages over the original C4 region



decoder [10]. First, it is implemented as a regular data path, in contrast to a linked-list structure, thus eliminating feedback and latency issues. Second, the output of the Block C4 region decoder is the control signal over an  $8 \times 8$  microblock, which lowers the output rate of the region decoder by 64, and reduces the power consumption. Finally, the length of the input of the region decoder is reduced from 51 bits  $(x, y, w, h, dir, dist)$  to 13 bits, i.e., 1-bit error location and 12-bit error value, and can be further packaged, resulting in fewer I/O pins in the decoder.

### Segmentation Predictor

As we stated previously, the segmentation predictor is the core of the region decoder. Its implementation is very similar to the linear predictor block with two exceptions: there is no microblock inputs for segmentation prediction, and the output has to be converted from the  $8 \times 8$  microblock domain to the pixel domain in the rasterized, i.e., left to right, top to bottom.

Figure 4.7 shows the schematics of the segmentation predictor. Note microblocks  $a$ ,  $b$ , and  $c$  of Figure 4.5 are now implemented as part of the delay chain of the output, resulting in a self-contained predictor. The output of the predictor may be replaced by the segmentation error value depending on the segmentation error location.

To convert the segmentation information to the pixel domain, we apply two delay blocks, each  $1024/8 = 128$  words long, in the predictor to relay the segmentation information within an  $8 \times 8$  block of pixels. As shown in Figure 4.7, the first delay block is used to keep track

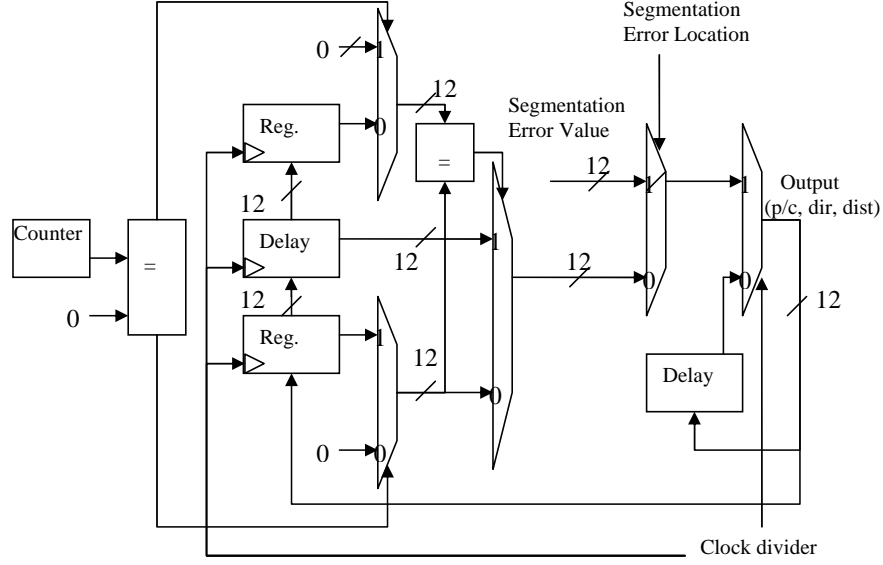


Figure 4.7: The block diagram of the segmentation predictor.

of microblock  $b$ ; thus it is only activated on the first row of every 8 rows of the pixels, and the clock rate is 8 times slower than the system clock, controlled by the clock divider; the second delay chain stores the decoded segmentation information from the predictor and circulates the information to generate the output for the following 7 rows of the pixels. As shown in Figure 4.8, the segmentation information of the yellow pixels is generated by the segmentation predictor, in which a delay chain is needed to keep track of the segmentation information from the yellow pixel above, and relayed to the 7 green pixels underneath by the second delay chain, while the whole block is operated at an 8-time slower clock rate, resulting in the remaining orange pixels. With this kind of decoding structure and a  $8\times$  clock divider, we can perform the segmentation prediction and maintain the integrity of the segmentation information within the microblock when the decoder decodes in the rasterized

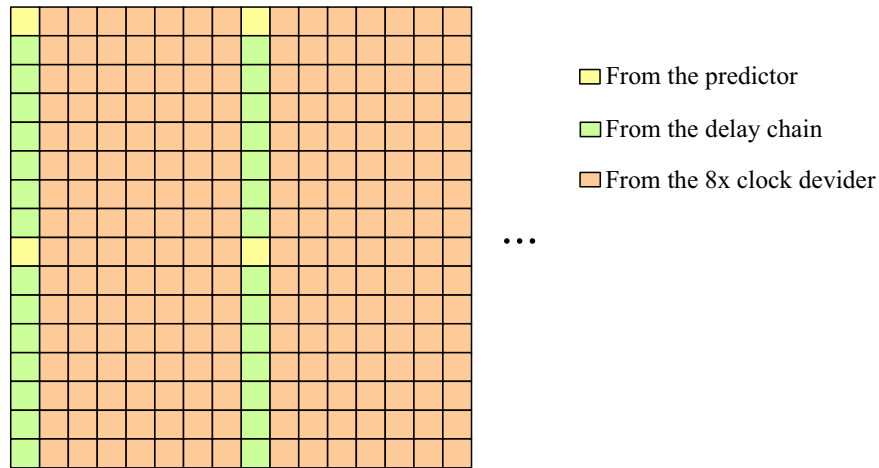


Figure 4.8: The illustration of converting segmentation information into the pixel domain.

order.

The delay chain can be implemented with either register files or SRAM. To reduce the hardware overhead of the decoder, we use a single-port SRAM block to implement the delay chain. Although it seems read and write operations are needed for every prediction, the region decoder block runs at the one-eighth of the system clock rate; as shown in Figure 4.9, read and write operations can be done in different clock cycles, and no extra buffering, data folding, or dual-port memory device is needed.

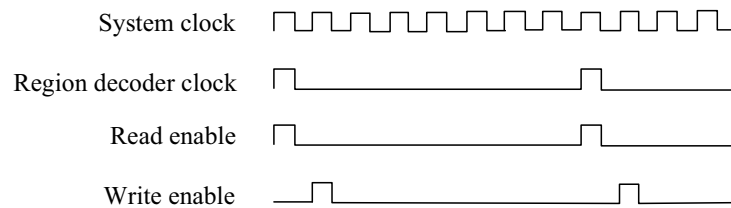


Figure 4.9: The timing diagram of the read/write operation of the delay chain.

## Golomb Run-Length Decoder

The design of a Golomb run-length decoder is adapted from techniques in the existing literature [39], as shown in Figure 4.10. It is the combination of a barrel shifter and a conventional run-length decoder. The barrel shifter is used as a data buffer to compact the coded error location into an 8-bit data stream, and the decoded result is used as the input to a run-length decoder, resulting in a binary output stream. In contrast to the approach in the literature, we only use one barrel shifter in our design to reduce the hardware overhead.

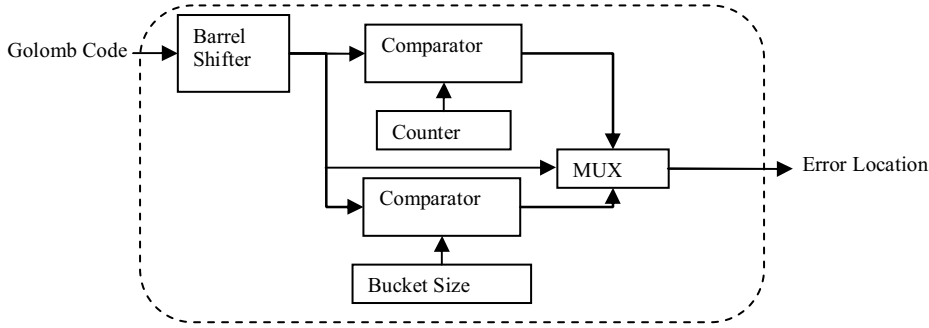


Figure 4.10: The block diagram of the Golomb run-length decoder.

### 4.2.3 Huffman Decoder

The Huffman code is a well-known entropy coding algorithm, and the Huffman decoder has been implemented in hardware [29]. For this design, the canonical Huffman algorithm is applied [44]. Unlike the traditional Huffman code [22], the canonical Huffman code arranges the codewords with the same code length in their original order. For example, if the symbol 1 and symbol 5 have the same codeword length, the codeword value of symbol 1 must be

smaller than the codeword value of symbol 5. While decoding canonical Huffman code, the codeword can be derived from arithmetic operations rather than pure table look-up, as in the traditional Huffman decoding. Hence it is easier to adapt the canonical Huffman decoder into a data-flow architecture.

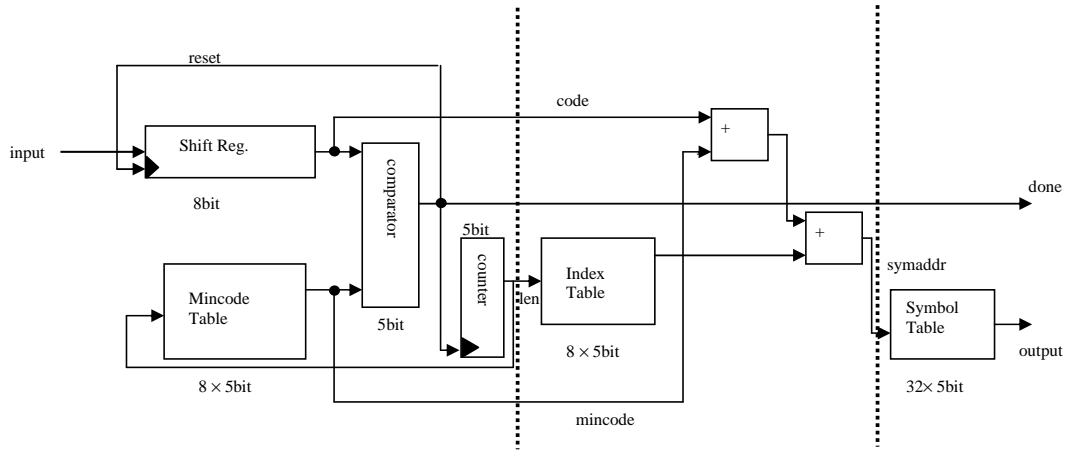


Figure 4.11: The block diagram of the Huffman decoder.

The block diagram of the Huffman decoder is shown in Figure 4.11. Basically, it can be divided into three stages and can be further pipelined if needed. At the first stage, the input goes into a shift register, and the counter is incremented by 1, which represents the tentative length of the codeword. The shifted input is then compared with the content in the Mincode table with the same length; if the shifted input is greater than the output from the Mincode table, the length of the current codeword is determined, and the shift register and the counter will be reset at the next clock cycle. After the length of the codeword is determined, the length information is used to address the Index table, which stores the offset

addresses of the codewords with the corresponding lengths. Finally, we add the offset value with the difference between the output of the Mincode table and the shifted input bit stream together; this represents the address of the Symbol table, in which the decompressed symbol is stored. The validity of the output signal is determined by the “done” signal, which can be treated as the write-enable signal for the output FIFO buffer.

The control of the Huffman decoder is fairly straightforward: the decoder keeps decompressing the input bitstream until the FIFO buffer is full, as shown in Figure 4.12. Under this structure, we do not even need a finite state machine to control this block; however, an enable signal is needed for all the sequential devices, such as the counter and the registers, to stall the block when the buffer is full.

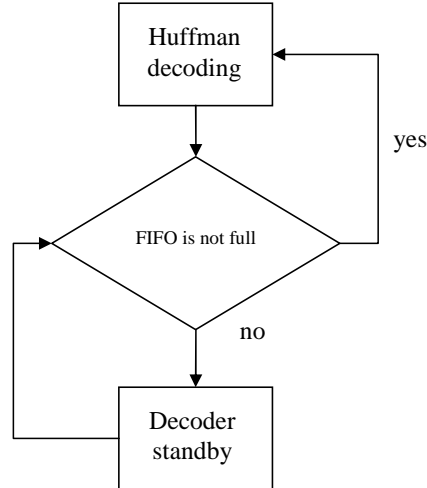


Figure 4.12: The control flow of the Huffman decoder.

Moreover, the hardware implementation overhead of the three look-up tables, Mincode, Index, and Symbol, are negligible due to several reasons: first, the size of these tables are

small, i.e., the total of 30 bytes; second, since the contents of the tables are fixed, for the reason stated in Section 3.4, we can implement them using combinational logics, so the area and the critical path can be optimized in the synthesis process.

#### 4.2.4 HCC Decoder

##### Architecture

Combinatorial coding (CC) is an algorithm for compressing a binary sequence of 0's and 1's [6]. For Block C4, it represents a binary pixel error location map. A “0” represents a correctly predicted or copied pixel, and a “1” represents a prediction/copy error. CC encodes this data by dividing the bit sequence into blocks of fixed size  $H$ , e.g.,  $H = 4$ , and computing  $k_{block}$  the number of “1”s in each block. If  $k_i = 0$ , this means block  $i$  has no ones, so it is encoded as 0000, with a single value  $k_i$ . If  $k_i > 0$ , e.g.,  $k_i = 1$ , then it needs to be disambiguated between the list of possible 4-bit sequences with one “1”: {1000, 0100, 0010, 0001}. This can be done with an integer representing an index into that list denoted  $rank_{block}$ . In this manner, any block  $i$  of  $H$  bits can be encoded as a pair of integers  $(k_i, rank_i)$ . The theoretical details of how this achieves compression can be found in [13], but intuitively it can be expressed as follows: if the data contains contiguous sequences of “0”s, and if the length of these all “0” sequences matches the block size  $H$ , each block of  $H$  “0”s can be concisely encoded as  $(k_i = 0)$  with no rank value, effectively compressing the data.

Computational complexity of CC grows as the factorial of the block size  $H$ . Hierarchical

combinatorial coding (HCC) avoids this issue by limiting  $H$  to a small value, and recursively applying CC to create a hierarchy [14], as shown in Figure 4.13.

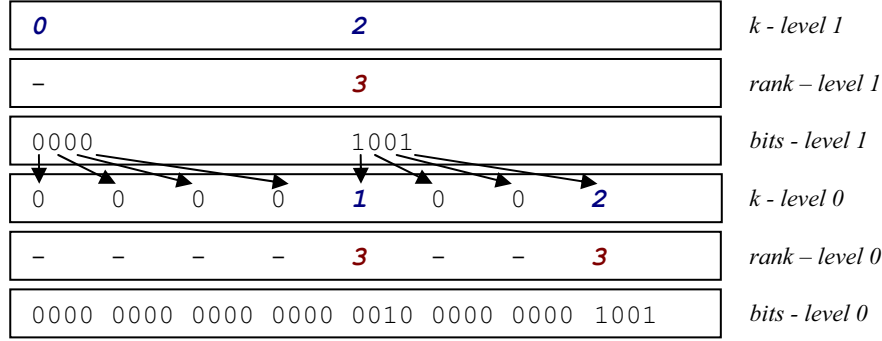


Figure 4.13: Two-level HCC with a block size  $H = 4$  for each level.

In Figure 4.13, the original binary sequence is the lowest row of the hierarchy “bits - level 0”. It has been encoded using CC as “ $k$  - level 0” and “rank - level 0” with a block size  $H = 4$ . We now recursively apply CC on top of CC by first converting the integers in “ $k$  - level 0” to binary “bits - level 1” as follows: 0 is represented as 0, and non-zero integers are represented as 1. Applying CC to “bits - level 1” results in “ $k$  - level 1” and “rank - level 1”. The advantage of the hierarchical representation is that a single 0 in “ $k$  - level 1” now represents 16 zeros in “bits - level 0”. In general, a single 0 in “ $k$  - level  $L$ ” corresponds to  $H^{L+1}$  zeroes in “bits - level 0”, compressing large blocks of 0’s more efficiently. The disadvantage of decoding the HCC is that it requires multiple CC decoding steps, as we traverse the hierarchy from top to bottom.

The task of traversing the hierarchy of HCC decoding turns out to be the main throughput bottleneck of HCC decoder, which in turn is the throughput bottleneck of the entire Block



C4 decoder. The block diagram of a sequential HCC decoder is shown in Figure 4.14(a). Block C4 uses a 3-level  $H = 8$  HCC decoder. The dashed lines separate the HCC levels from top to bottom, and the data that moves between levels are the bits - level  $L$ . Three CC blocks represent  $(k, rank)$  decoders for levels 2, 1, and 0, from top to bottom respectively. CC - level 2 decodes to bits - level 2. If *bits* - level 2 is a “0” bit, the MUX selects the run-length decoder (RLD) block which generates 8 zeros for bits - level 1. Otherwise, the MUX selects the CC - level 1 block to decode a  $(k, rank)$  pair. Likewise, bits, level - 1 controls the MUX in level 0. A “0” causes the RLD block to generate 8 zeros, and a “1” causes CC - level 0 to decode a  $(k, rank)$  pair. In this sequential design, the output of a lower level must wait for the output of a higher level to be available before it can continue. Consequently, the control signal corresponding to when the output of the lowest level bits level - 0 is ready resembles Figure 4.14(c). While levels 2 and 1 are decoding as indicated by the shaded boxes, the output of layer 0 must stall, reducing the effective overall throughput of the HCC block.

To overcome the problem of hierarchical HCC decoding, we can parallelize the operation by introducing a FIFO buffer between HCC levels, as indicated by the additional squares in Figure 4.14(b), and by dividing the input  $(k, rank)$  values for each HCC level into multiple sub-streams. The idea is that after an initial delay to fill the buffers of levels 2 and 1, level 0 can decode continuously as long as the buffers are not empty. This is guaranteed because one level 2 output bit corresponds to 8 level 1 output bits, and 64 level 0 output bits. Level 2 and level 1 can continue to decode into these buffers while level 0 is operating. Consequently, the

output control signal of the parallel design resembles Figure 4.14(d), where only the initial delay is noticeable. The control mechanism of the parallel design is also considerably simpler than the sequential design, because each HCC level can now be controlled independently of the other HCC levels, halting only when its output buffer is full, or its input buffer is empty. Only a 2-byte FIFO is introduced between each level. However, the throughput of the HCC decoder is still less than a typical data flow due to the iterative and complicated decoding process.

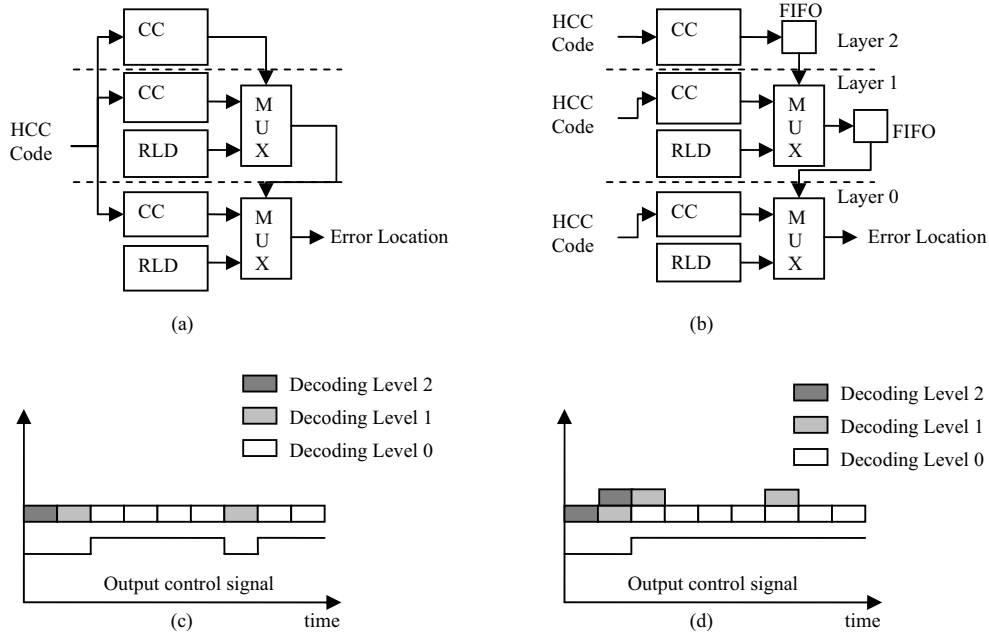


Figure 4.14: The decoding process of HCC in (a) top-to-bottom fashion and (b) parallel scheme. The timing analysis of (c) top-to-bottom fashion and (d) parallel scheme.

With this decoding architecture, each level of the HCC decoder is controlled by a Mealy state machine [23]. The decoding flow is shown in Figure 4.15, where for each level, the decoding process is triggered by the output of the upper level; an input of 1-bit “1” enables

the Huffman–Uniform–Combinatorial decoding process, since the  $(k, rank)$  pairs are coded with Huffman code and uniform code respectively. The operation of these three decoding blocks are illustrated in the following subsections.

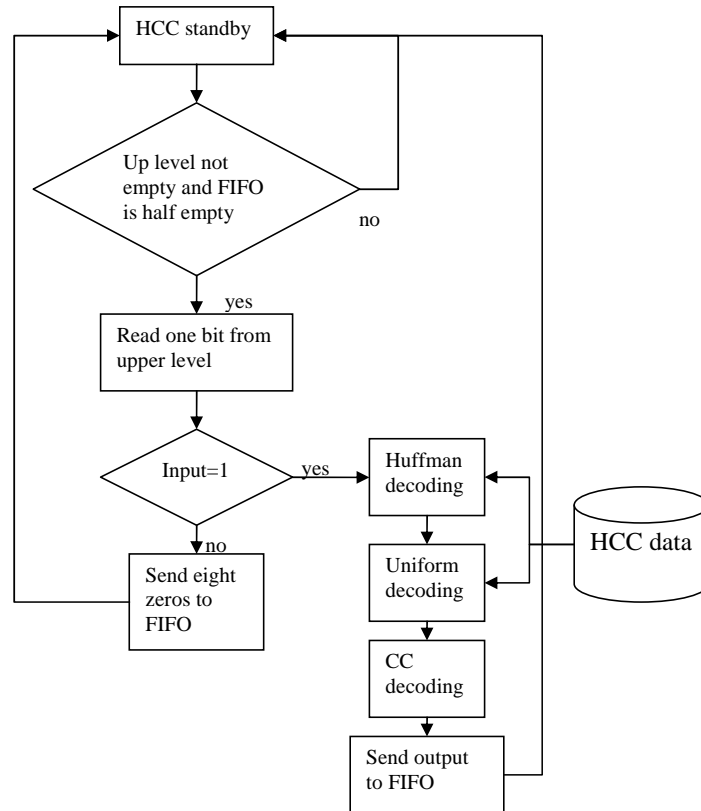


Figure 4.15: The control flow for one level of the HCC decoder.

## Huffman Decoder

For each  $(k, rank)$  pair, the parameter  $k$  is coded with Huffman code, due to the fact  $k$  is skewed toward the lower values. The design of the Huffman decoder inside the HCC decoder is mainly the same as the one described in Section 4.2.3, with the exception of different

look-up tables for each level. These look-up tables also need to be updated for different images, for their different image error location distributions. This can introduce extra data stream overhead for the decoder design.

### Uniform Decoder

For a certain value of  $k$ , the corresponding *rank* is within the range of  $[0, {}_8C_k - 1]$ . Therefore, the codeword length for *rank* should be the ceiling value of  $\log_2({}_8C_k)$ , which is denoted to be the code length  $L$  for  $k$ ; all *rank* values with the same  $k$  can be coded with either  $L - 1$  bits or  $L$  bits. In order to save bits, the *ranks* are folded back along a threshold value  $m$ . Below the threshold, the rank values are coded with  $L - 1$  bits. This is called uniform coding.

The decoding process is very straightforward. Corresponding to a certain  $k$ , the decoder reads the first  $L - 1$  bits from the input bit stream and compares the value in the threshold table. If it is less than  $m$ , the decoder sends out the value of the stream and claims the “done” signal; otherwise, it reads another bit and subtracts  $m$  from the bit stream. Figure 4.17 shows the schematic for the uniform decoder. The values in the look-up tables are fixed, and can thus be implemented with ROMs or combinational logics. The outputs of this block are the 1-bit “done” signal and the 8-bit *rank* value, which is sent to the combinatorial decoder.

*Encode:*

$$n \in [0, \text{rank}], \text{rank} \in \mathbb{N}$$

Let  $L = \lceil \log_2 \text{rank} \rceil$ ,  $m = 2^L - \text{rank} + 1$

$$\text{Encode}(n) = \begin{cases} n & \text{with } L - 1 \text{ bits} & \text{if } 0 \leq n < m \\ n + m & \text{with } L \text{ bits} & \text{if } m \leq n < 2^L \end{cases}$$

*Decode:*

$$\text{Decode}(n) = \begin{cases} r & \text{if } \text{Read}(r, L - 1 \text{ bit}) < m \\ \text{Read}(r, L \text{ bit}) - m & \text{otherwise} \end{cases}$$

Figure 4.16: The encoding/decoding algorithm for uniform coding.

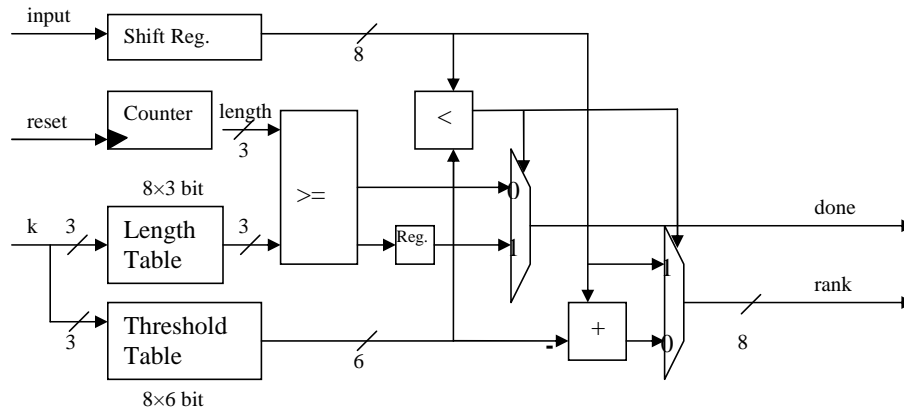


Figure 4.17: The schematic of the uniform decoder.

## Combinatorial Decoder

The combinatorial coding is a version of enumerative coding [6]. For a fixed blocked size of  $M$ ,  $k$  represents the number of ones inside the block. In Block C4,  $M = 8$ . For a certain

$k$ , all the possible combinations are ordered for 0 to  ${}_8C_k - 1$ , according to their values. For example, with four ones in eight bits, “00001111” is ranked as 0, where “11110000” is ranked as 69. In short, the pair  $(k, rank)$  represents all possible sequences inside the 8-bit block.

The decoding scheme is described in [6]. In principle,  $rank$  is decomposed into the summation of combinations by Pascal’s triangle. For instance, the sequence “11110000” with  $rank = 69$  can be decomposed into  ${}_7C_4 + {}_6C_3 + {}_5C_2 + {}_4C_1 = 35 + 20 + 10 + 4$ , which implies the decoding process is done by decomposing the rank value with Pascal’s triangle.

The decoder operates as follows: the internal parameter  $n$  is initialized to 7. For every iteration, the  $rank$  value is compared with the value  ${}_nC_k$ , which is stored in the CC table. If  $rank \geq {}_nC_k$ , the output is “1”, and the value  $k$  is updated with  $k - 1$ ; otherwise the output is “0”, which suggests the ones appear later in the sequence, and then the value  ${}_nC_k$  is subtracted from  $rank$ . Every iteration ends with the update of  $n = n - 1$ , and the decoding process ends when  $rank$  reaches zero. Besides the CC table, the offsets of address for each  $k$  value are held in the index table. The contents of the tables are fixed, thus the look-up tables can be implemented in ROMs. The output of this block is the binary bit stream with size 8 and a “done” signal. The flow chart is shown in Figure 4.18, and the schematic of the hardware design is shown in Figure 4.19. The output of the CC decoder is generated every clock cycle, with a latency of two clock cycles. This is due to the one-clock cycle delay of each memory block.

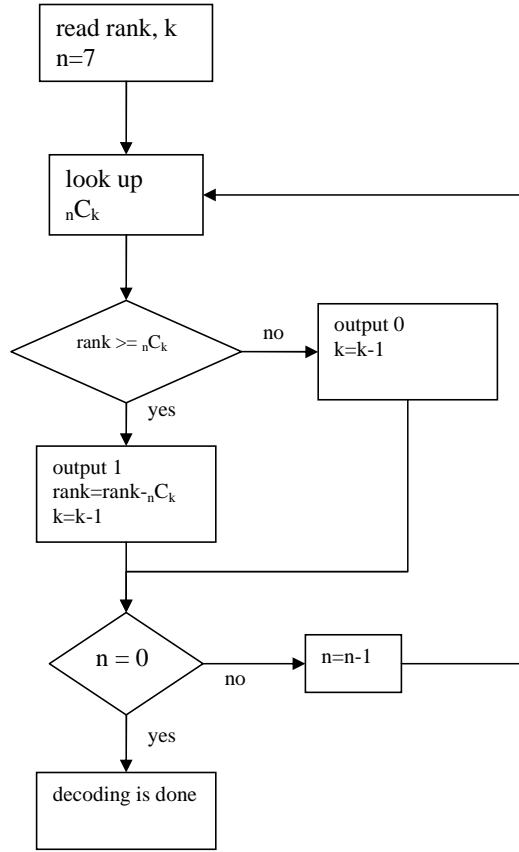


Figure 4.18: The decoding flow of the combinatorial decoding.

### 4.2.5 Address Generator

The address generator computes of two kinds of addresses, the prediction address and the copy address, to access the history buffer. The prediction address denotes the address for pixel  $b$  in Figure 4.4, i.e., (*current address* - 1024); on the other hand, the copy address, depending on the copy direction, randomly accesses the history buffer. Notice there is an extra “transition” signal, which denotes the segmentation switching from a copy region to a prediction region. In this case, the decoder has to read the values of both pixel  $a$  and pixel

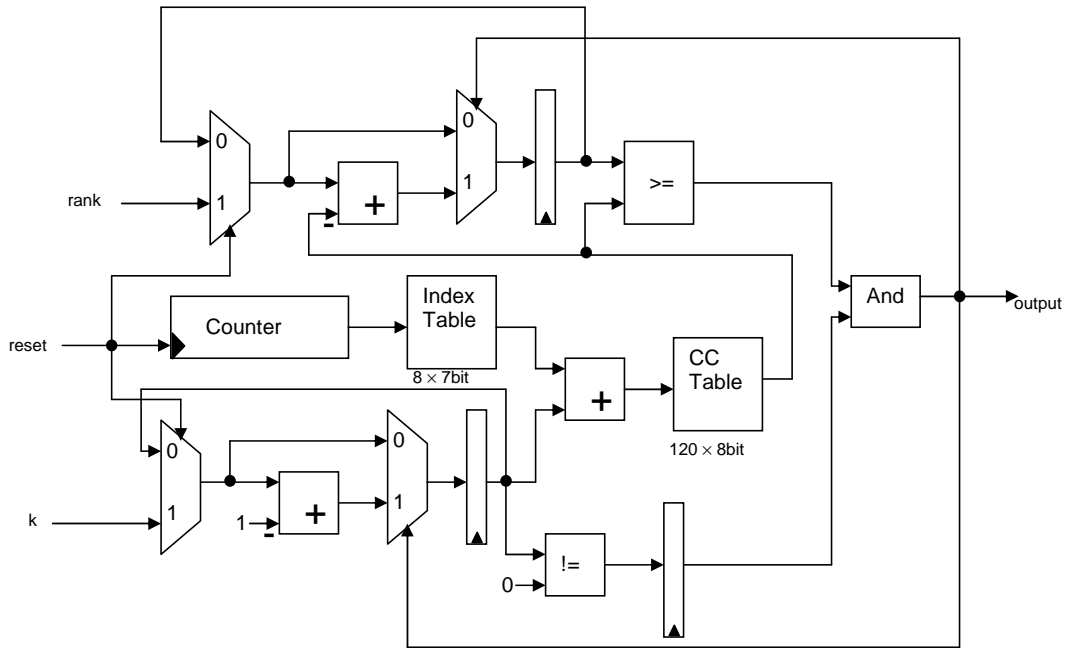


Figure 4.19: The schematic of the combinatorial decoder.

$b$  before performing linear prediction. This extra operation is caused by the shared history buffer for both linear prediction and copy method. The schematic of the address generator is shown in Figure 4.20.

### 4.2.6 Control Unit

This is the final stage of the decoder, where all the signals are collected to select the output pixel value. The schematic is shown in Figure 4.21. This block can be implemented in the pipelined structure. In the actual implementation, the process is pipelined into three stages. At the first stage, the control block detects that the buffers for the Huffman decoder is not empty; in this case, the block sends out an enable signal to start decoding, with



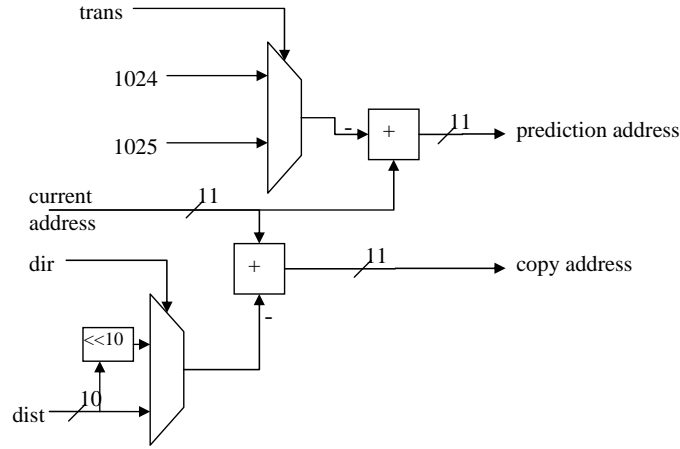


Figure 4.20: The block diagram of the address generator.

the exception of the transition from a copy block to a predicting block, as described in Section 4.2.5. At the second stage, the output from the address generator, the prediction address and copy address, are selected by the “ $p/c$ ” signal from the region decoder, and the output is sent to history buffer to access the corresponding pixel values in the buffer. Meanwhile, the decoded error location is read as a control signal to read the decompressed error value from Huffman decoder. At the final stage, the outputs from linear prediction, history buffer, and Huffman decoder are merged and the output of the decoder is selected with the mechanism shown in Figure 4.2. Meanwhile, the system sends out a “done” signal as a handshaking token for the writer system, and the output pixel values are stored into a register as the value of pixel  $c$  for the linear prediction at the next clock cycle; the same output pixel value is also stored into the history buffer for future use.

Basically, the decoding throughput is determined by the throughput of HCC block, with the exception of copy/prediction transition. In the transition case, the system needs one

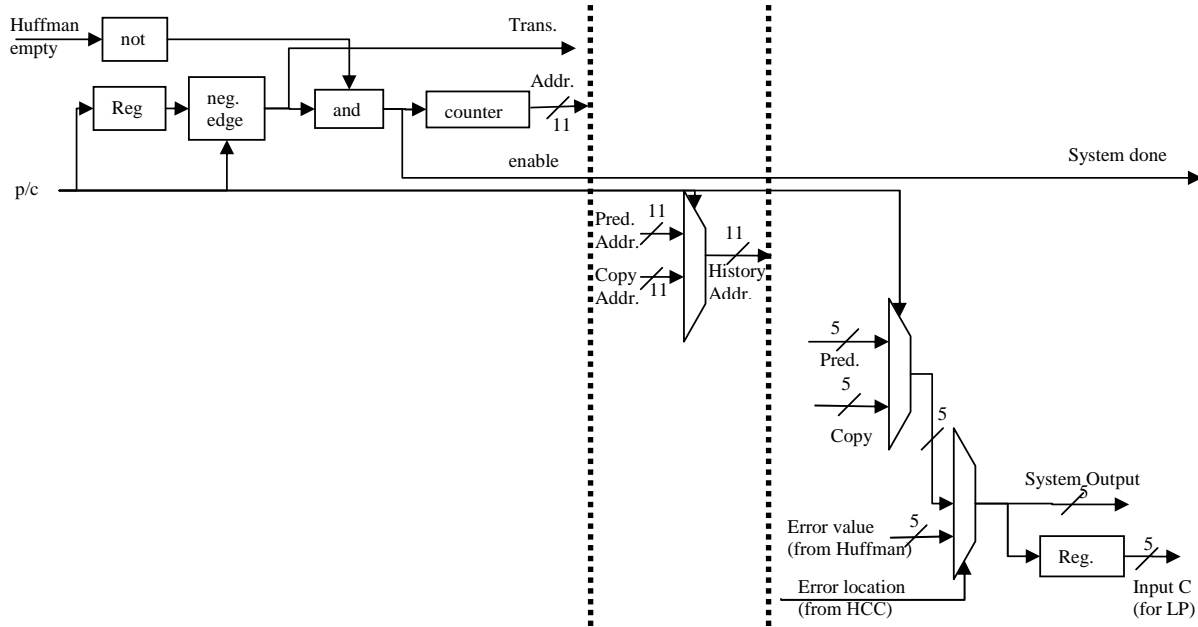


Figure 4.21: The detail block diagram of the control block.

extra clock cycle to read from the history buffer to get the values of pixels  $a$  and  $b$ .

### 4.2.7 On-Chip Buffering

There are three major buffer blocks in Block C4 decoder: The delay chains inside the region decoder, the History block shown in Figure 4.1, and the internal FIFO buffer. Among them, we have already discussed the implementation of the delay chains in Section 4.2.2 In this subsection, the other two buffer designs are presented.

## History Block

This block is the major memory block, storing the pixel values from the previous 2048 samples, equivalent of two rows for the  $1024 \times 1024$  images. Nevertheless, the design of this block is trivial; it consists of mainly a  $2048 \times 5$  dual-port memory, one port for the reading process and one port for the writing process. However, due to the pipelining in the control block, the data handling of this block has to prevent false data accessing as the pixel value of the last pixel has not been written into the buffer yet.

## FIFO Buffer

Since the Huffman decoder generates a 5-bit output every 3–7 clock cycles, depending on the codeword length, the FIFO buffer is applied to balance the varying output rate of the Huffman decoder. As long as the FIFO is not drained to be empty, the output of the FIFO can be treated as a regular data storage device that can provide the 5-bit image error value steadily for every residue pixel. In this case, the size of the FIFO becomes critical: it has to be large enough to guarantee that the FIFO can never be drained to be empty, but it cannot be too large to increase the unnecessary hardware overhead. We empirically determine its size to be  $64 \times 5$ , which is negligible as compared with the history buffer.

The block diagram of the synchronous FIFO design, adapted from literature [46], is shown in Figure 4.22. There are two counters, triggered by the read and write enable signals, tracking the read and write statuses of the dual-port memory respectively. The corresponding addresses are used to generate the “full” and “% Full” flags, as the control

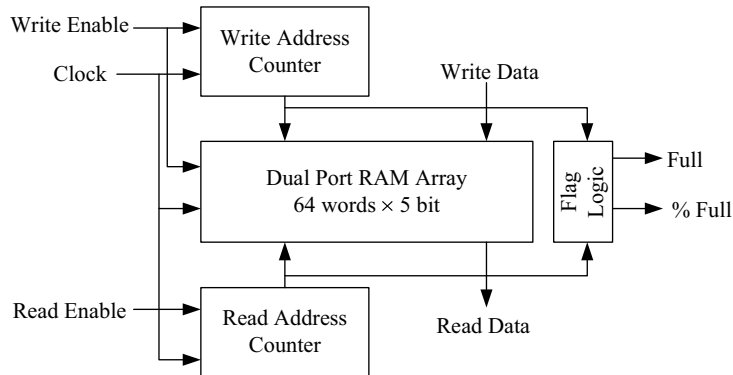


Figure 4.22: The detail block diagram of the synchronous FIFO.

signals for the control block and Huffman decoder. For example, if there is only one unwritten word in the array and the “write enable” is active, the “full” flag will be “1” at the next clock cycle. The dual-port memory is synchronized by the system clock, and the output is latched by a register, so the output “read data” can be ready with one clock cycle latency.

### 4.3 Block GC3

Since the pixel error location in Block GC3 is encoded with Golomb run-length coder, the pixel error location decoder of Block GC3 resembles the Golomb run-length decoder for the segmentation map in the Region Decoder of Block C4. However, for pixel error locations, it is advantageous to use a variable bucket size in the Golomb run-length coder for different process layers in order to improve compression efficiency, as discussed in Chapter 3. The block diagram of Golomb run-length decoder for error location is shown in Figure 4.23. The only difference between Figures 4.10 and 4.23 is that the variable bucket size is introduced as

an input signal to the decoder. The main advantage of this implementation over HCC is that it has zero latency, and does not require any stall cycles during the decoding process due to its regular data-flow structure. Besides, Golomb run-length decoder is nine times smaller than HCC decoder in terms of hardware implementation, as well as less power consumption and higher throughput. Table 4.1 shows an estimated ASIC hardware performance comparison between Block C4 and Block GC3, in a general-purpose 90 nm technology. It is clear the simplicity of Block GC3 in terms of hardware implementation more than compensates for its compression efficiency loss as discussed in Section 3.2. As a result, we choose to focus on implementing Block GC3 decoder on FPGA and ASIC in the following sections.

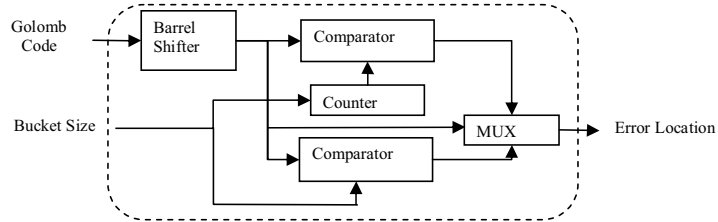


Figure 4.23: The block diagram of the Golomb run-length decoder.

## 4.4 FPGA Emulation Results

We implement Block GC3 decoder in Simulink-based design flow, then synthesize and map onto the FPGA. We use Xilinx Virtex II Pro 70 FPGA, part of the Berkeley Emulation Engine 2 (BEE2), as our test platform [3]. Figure 4.24(a) shows the picture of the BEE2 system, and Figure 4.24(b) shows the schematic of Block GC3 emulation architecture. BEE2

Table 4.1: Estimated hardware performance comparison of different data path of direct-write maskless lithography systems.

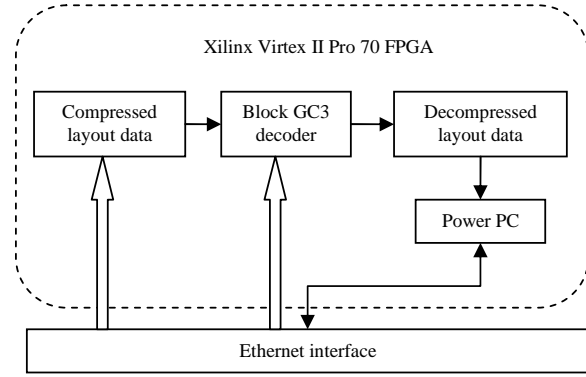
Block	Area ( $\mu m^2$ )	Throughput	
		(output/cycle)	Power (mW)
Golomb	4845	1	1.8
HCC	43,135	0.71	7.4
Block C4	100,665	0.71	24.6
Block GC3	62,375	0.94	19.1

consists of five FPGAs and the peripheral circuitry, including Ethernet connections, which are used as communication interface in our emulations. Since Block GC3 decoder is deliberately designed to be of low complexity, only one FPGA is utilized. Inside this FPGA, the design of Block GC3 decoder is synthesized and mapped, and the compressed layout data is stored into additional memory. After decoding, the decoded layout data is stored, and can be accessed by the user through the Power PC embedded in the FPGA, under the BORPH operating system [37]. Using this architecture, we can easily modify the design and verify its functionality [28].

Table 4.2 shows the synthesis results of Block GC3 decoder. Only 3233 slice flip flops and 3086 4-input look-up tables (LUTs) are used, which correspond to 4% of the overall FPGA resources. In addition, 36 Block RAMs are utilized, mainly to implement the 1.7 KB internal memory of Block GC3 decoder and I/O registers. The system is tested at 100 MHz clock rate, which accommodates the critical data path of the system after synthesis.



(a)



(b)

Figure 4.24: (a)The BEE2 system [19]; (b) FPGA emulation architecture of Block GC3 decoder.

Table 4.2: Synthesis summary of Block GC3 decoder.

Device	Xilinx Virtex II Pro 70
Number of slice flip-flops	3,233 (4%)
Number of 4 input LUTs	3,086 (4%)
Number of block RAMs	36 (10%)
System clock rate	100 MHz
System throughput rate	0.99 (pixel/clock cycle)
System output data rate	495 Mb/s

Through empirical testing, we find the internal buffer can be further reduced to 1 KB. Using the 2-row search range, the vertical copy can be fully replaced by prediction to achieve the same performance. In doing so, the data in the previous row is not needed, and the search range can be reduced to 1-row. This memory reduction may result in lower compression

efficiency if the image is extremely hard to either predict or copy. However, for our test images, this never occurs.

By decompressing the actual layout images, we measure the actual throughput of the system. Unlike the previous estimate in [3], the actual system throughput is 0.99 pixels/clock cycle. The system only stalls in the transition from a copy region to a predict region, and in practical scenarios, this only happens 1% of the time. Combining the 100 MHz clock rate, 0.99 system throughput, and 5 bit/pixel output data type, the system output rate is 495 Mb/s. By switching the implementation platform from FPGA to ASIC, the clock rate can be further improved, resulting in a higher output data rate for each decoder.

## 4.5 ASIC Synthesis and Simulation Results

To improve the performance of Block GC3 decoder and to study its integration with the writer chip, we synthesize the decoder design using logic synthesis tools in a general-purpose 65 nm bulk CMOS technology for ASIC implementations. The design is synthesized on the slow, typical, and fast corners of the standard cell library, with the target clock rates of 220, 330, and 500 MHz respectively. The synthesized gate-level decoder is verified for its functionality and accurate power estimates are obtained [28].

The synthesis results are shown in Table 4.3, with the area and power broken down by blocks for analysis purposes. Under the three synthesis environment settings, the area of a single Block GC3 decoder remains approximately the same, with 85% of the area devoted to the memory part of the design, i.e., 2 KB dual-port SRAM for the history buffer, 192 B



Table 4.3: ASIC synthesis result of Block GC3 decoder.

Block	Slow corner, 125 °C		Typical corner, 25 °C		Fast corner, 125 °C	
	Area ( $\mu\text{m}^2$ )	Power (mW)	Area ( $\mu\text{m}^2$ )	Power (mW)	Area ( $\mu\text{m}^2$ )	Power (mW)
Address	358.8	0.0149	61.9	0.0361	358.8	0.0356
Generator						
Control	873.6	0.111	748.8	0.215	749.3	0.221
Golomb	1146.1	0.0864	1135.7	0.201	1137.8	0.219
RLD						
History	36977.7	5.079	36954.3	8.802	36954.3	10.342
Buffer						
Huffman	850.2	0.0924	848.1	0.207	848.1	0.223
Linear	593.32	0.0975	455.0	0.155	500.8	0.197
Predictor						
FIFO	10075.7	2.543	10005.5	4.47	10011.7	5.137
Region	18380.5	4.09	18370.1	7.26	18371.7	8.054
Decoder						
Total	69668.3	12.16	69288.2	21.482	69342.8	24.573

dual-port SRAM for the internal FIFO, and 512 B single-port SRAM for the region decoder.

The logic and arithmetic parts of the system which have been optimized at the architecture level, contribute to 15% of the area. Notice the memory size is greater than the designed 1.7 KB because we choose the memory blocks from the library with the closest dimensions. If

custom-designed memory blocks were used, the area of the decoder could have been further reduced.

The memory blocks also contribute to the critical path of the system, namely the “history buffer–linear predictor–control–history buffer” path as shown in Figure 4.1. Since this path involves both the read and write processes of the dual-port memory, the access time of both operations has to be considered, along with the propagation delays from other logic and arithmetic operations. This results in a relatively slow clock rate for the 65 nm technology; nevertheless, the impact may also be alleviated by applying custom-designed memory blocks.

The power consumption in Table 4.3 is estimated by decoding a poly layer layout image and recording the switching activities of the decoder during the process. Intuitively, a faster clock rate results in a higher switch activity; this phenomenon is reflected in the power consumption, as the fast corner design consumes more power than the other two designs. However, this number may vary from image to image, since for the sparse layouts or non-critical layers of the layouts, the switching activity may be much lower than that of the poly layer. In fact, if we use an average 25% switching activity factor to estimate the power, the difference can be up to 75%.

Table 4.4 shows samples of power estimate using different environment settings and switching activity factors ( $\alpha$ ). Notice the power estimate for decoding the poly layer image is much higher than the power estimate assuming  $\alpha = 0.25$ ; in particular, the most discrepancy happens in the address generator block, where the switching activity is much higher than 25%. This is due to the incremental operation of the binary counter; the correspond-

Table 4.4: Power estimate of Block GC3 decoder with different switching activity factors  $\alpha$  .

Block	Typical corner power(mW)		Fast corner power (mW)	
	$\alpha = 0.25$	Decoding poly layout	$\alpha = 0.25$	Decoding poly layout
Address	8.26 E <sup>-5</sup>	0.0361	0.00439	0.0356
Generator				
Control	0.124	0.215	0.203	0.221
Golomb	0.132	0.201	0.217	0.219
RLD				
History	5.172	8.802	9.312	10.342
Buffer				
Huffman	0.127	0.207	0.203	0.223
Linear	0.0213	0.155	0.0388	0.197
Predictor				
FIFO	2.682	4.47	4.641	5.137
Region	4.41	7.26	7.352	8.054
Decoder				
Total	12.771	21.482	22.14	24.573

ing switching activity can be reduced by replacing the binary counter with the Gray code counter.

With the synthesis results shown in Table 4.3, the ASIC implementation of a single Block

GC3 decoder can achieve the output data rate up to 2.47 Gb/s. For 200 decoders running in parallel, resulting in the total output rate of 500 Gb/s, or 3 wafer layers per hour, the required area and power are  $14\text{ mm}^2$  and 5.4 W respectively. As compared to the direct-write method, this results in a power saving of 24% with a minimal amount of hardware overhead [4]. However, in terms of layout floorplanning, the aspect ratio of the decoder layout has to be further determined, depending on different writer system architectures and layout specifications, such as in [40] and [33].

## 4.6 Summary

In this chapter, we have shown the detailed implementation of Block C4 and Block GC3 decoder, with the schematic and operation of each blocks. Between these two designs, we choose to implement Block GC3 in both FPGA and ASIC. For FPGA, a single Block GC3 decoder only utilizes 4% of the resources of a Xilinx Virtex Pro II 70 FPGA. The system can run at 100 MHz, resulting in an output data rate of 495 Mb/s. We have also presented the ASIC synthesis result of the design in the 65 nm technology, which results in a  $0.07\text{ mm}^2$  design with the maximum output data rate of 2.47 Gb/s for a single decoder. Its low hardware overhead and data flow architecture make it feasible for parallel processing of direct-write lithography writing systems.

## Chapter 5

# Integrating Decoder with Maskless Writing System

### 5.1 Introduction

In order to integrate the Block GC3 decoder with the writer system, we have to consider the datapath between the decoder and the rest of the system. This includes buffering the data from the I/O interface to the decoder, buffering the output of the decoder before it is fed into the writer, and packaging the input data stream so that multiple input data streams can share the same I/O interface. In addition, since the Block GC3 uses previous output data to either predict or generate the current pixel value, proper error control is needed to avoid the error propagation. These issues are discussed in this chapter.

## 5.2 Input/Output data buffering

In Block GC3 decoder, one bit in the input data stream is typically decoded into multiple output pixel values, depending on the compression efficiency. In other words, the input data rate is potentially lower than the output data rate by the compression ratio, resulting in a fewer number of input data links and lower power consumption by the I/O interface. In practice, this lower input data rate can only be achieved by buffering the input data on-chip before it is read by the decoder. However, this also requires additional internal buffers of the writer chip, which is what we are trying to avoid in the first place. In previous work, we have proposed the on-chip buffer to be of the size

$$\text{buffer size} = \frac{\text{image size}}{\text{compression ratio}}, \quad (5.1)$$

which suggests the entire  $1024 \times 1024$  compressed layout image to be stored in the memory before being decoded [47]. Assuming the compression ratio of 10, this corresponds to 64 KB of internal buffer. Even though this number is not substantial, considering hundreds of decoders running in parallel to achieve the projected output data rate, the scaled buffer size may not be feasible. In addition, this buffer size may be an overestimate since the writer system reads and writes the buffer simultaneously, in a first-in-first-out fashion. In this case, the buffer may only be completely full at the very beginning of the decoding process, resulting in a waste of the resources.

To circumvent the above problem, we propose to reduce the size of the input data buffer

to

$$\text{buffer size} = a \times \text{image size} \times \left( \frac{1}{\text{compression ratio}} - \frac{1}{\text{input data rate}} \right). \quad (5.2)$$

Unlike Eqn. (5.1), the buffer size in Eqn. (5.2) is a function of both the input and output rate of the FIFO, and the size is reduced by taking the update speed into account. The constant  $a$ , which is slightly greater than 1, is introduced to ensure the FIFO will not become empty. For high compression ratio images, this buffer will always be almost full, since the input data rate is higher than the compression ratio, which corresponds to the output data rate. In this case, the input data link is on only when the FIFO is not full. On the other hand, for low compression ratio images, the FIFO is slowly drained to be empty; this is because its output data rate is higher than its input data rate, while the input data link is always on, running at the designed input data rate. In this architecture, after decomposing the rasterized layout into a series of images, we need to arrange the layout images so that not all low compression ratio images are clustered together, resulting in an empty input FIFO. The arrangement strategy for layout images was presented in [47], and can be performed at the encoding stage.

### 5.3 Control of Error Propagation

In Block GC3 algorithm, both copy and predict schemes use the previous pixel values stored in the history buffer to generate the current pixel value. If the stored pixel value is altered during the read/write process of the history buffer, the error propagates to the

remaining part of the image. To solve this problem, we have to consider error control strategies. First, the history buffer has to be refreshed for every new image. Although Block GC3 algorithm is suitable for stream coding, i.e., using the history buffer of the previous image to code the current one, the error can also propagate from the previous image in the same fashion. Therefore, refreshing of the history buffer would confine the error to the image boundaries. This results in some encoding overhead at the beginning of the images, and lower compression efficiency as compared to stream coding. However, considering the 1-row and 2-row buffer cases, the overhead and compression efficiency loss are negligible.

Besides setting up the boundaries of the images, we can further reduce error by applying error control code (ECC) to the history buffer. Hamming (7, 4) code is a simple error control code, which has been implemented in hardware in the literature [26] [43]. In this code, 4 bits of data are coded with 3 extra parity bits to construct a 7-bit code. While decoding the Hamming code, one error bit in the code can be identified and corrected, and two error bits can be detected by the decoder. In the history buffer of Block GC3, we can apply the Hamming (7, 4) code to encode the four most significant bits of the 5-bit pixel value, resulting in a 8-bit code for every pixel, which can be stored into a typical memory design without wasting resources. While reading the pixel value from the history buffer, the single-bit error can be corrected. A schematic of possible history buffer design is shown in Figure 5.1. Depending on the retention ability of the memory, this may effectively reduce the error propagation.



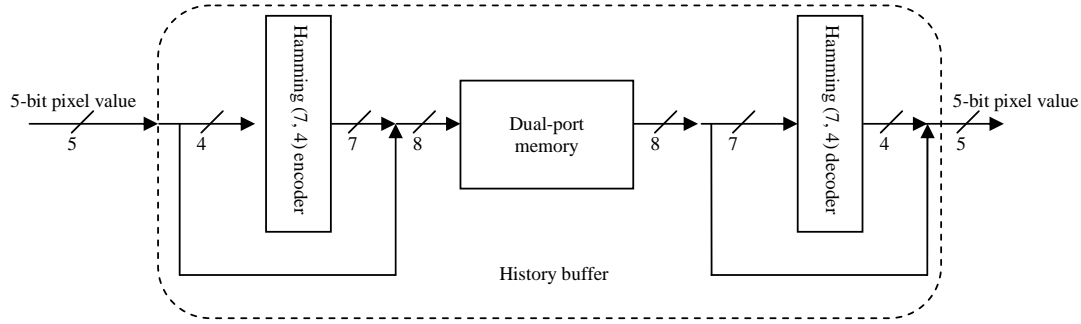


Figure 5.1: The block diagram of the history buffer with ECC.

## 5.4 Data Packaging

In our FPGA implementation, all the compressed data streams are stored separately and sent to the region decoder, Golomb run-length decoder, and Huffman decoder of Block GC3 decoder simultaneously in order to demonstrate the data-flow type of decoding process. In order to reduce the number of input data links, these data streams can be combined into one. However, not all the data streams are read at the same rate; for example, the segmentation information is needed at most per 64 pixels, whereas the compressed error location is read at most every 2 pixels. Therefore, in order to pack the input data stream, the Block GC3 encoder has to mimic the decoding process and arrange the data stream accordingly. This may introduce extra encoding overhead; however, since the decoding process is two to three orders of magnitude faster than the encoding, the impact is marginal. In addition, in the Block GC3 decoder, the input data stream for each block has to be further buffered to balance the data requests among different blocks, in case they send out the read requests at the same time. This extra buffer can be only several bytes and implemented in FIFO, but

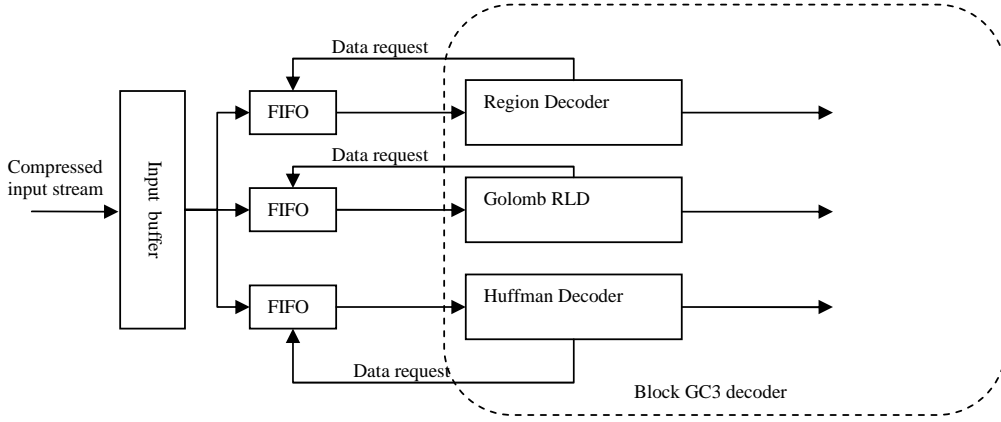


Figure 5.2: Data distribution architecture of Block GC3 decoder

it is essential for each decoding block to unpack the input data stream in this architecture, as shown in Figure 5.2.

## 5.5 Summary

With these synthesis results and data-flow architecture of the decoder, it is potentially feasible to run hundreds of Block GC3 decoders in parallel to achieve the high-throughput needed for direct-write lithography systems. In order to integrate the decoder in the path, we also propose a number of data handling strategies in this chapter.

However, this is only the first step toward the integrating the Block GC3 decoder into the direct-write lithography writer systems. For the final realization, we still have to explore the scalability and multi-thread data handling challenges of the parallel decoding systems, in both performance and design aspects. In addition, since Block GC3 is a generic lossless compression algorithm for direct-write lithography systems, we may have to modify the

algorithm to accommodate the specifications of different writing technologies and layout images while keeping the decoder complexity low. In the next chapter, we will provide one such writing system as a case study.

## Chapter 6

### Block RGC3: Lossless Compression

### Algorithm for Rotary Writing

### Systems

#### 6.1 Introduction

A new maskless direct-write lithography system, called Reflective Electron Beam Lithography (REBL), is currently under development at KLA-Tencor [33]. In this system, the layout patterns are written on a rotary writing stage, resulting in layout data which is rotated at arbitrary angles with respect to the pixel grid. Moreover, the data is subjected to E-beam proximity correction effects. We have empirically found that applying the Block GC3 algorithm to E-beam proximity corrected and rotated layout data results in poor com-

pression efficiency far below those obtained on Manhattan geometry and without E-beam proximity correction. Consequently, Block GC3 needs to be modified to accommodate the characteristics of REBL data while maintaining a low-complexity decoder for the hardware implementation. In this chapter, we modify Block GC3 in a number of ways in order to make it applicable to the REBL system; we refer to this new algorithm as Block Rotated Golomb Context Copy Coding (Block RGC3).

In this chapter, we first introduce the data-delivery path of the REBL system and the requirements it imposes on the compression technique. We then describe the modifications resulting in Block RGC3; these include an alternate copy algorithm, a finer block size, and segmentation information compression, which better suit rotated layout patterns. We also characterize the additional encoding complexity required to implement our proposed changes to Block GC3.

## 6.2 Datapath for REBL System

The REBL system is visualized in Figure 6.1(a), and detailed in [33] [32]. REBL’s goal is to produce high resolution of electron-beam lithography while maintaining throughputs comparable to those of today’s optical lithography systems. The Digital Pattern Generator (DPG) uses reflective electron optics to constantly shape the electron beam as it scans across the wafers, which are located on a rotary stage shown in Figure 6.1(b). This chapter focuses on the data delivery path of the REBL system, which constrains the compression hardware implementation. As shown in Figure 6.2, the compressed layout data is decoded by Block

GC3 decoders in parallel, and then fed into the DPG, which can be located on the same chip as the decoder. In order to meet the required minimum wafer layer throughput of the REBL system, namely 5–7 wafer layers per hour (WPH), given the data rate of the available optical input data link of about 10Gb/s/link, a required minimum compression ratio of 5 is projected.

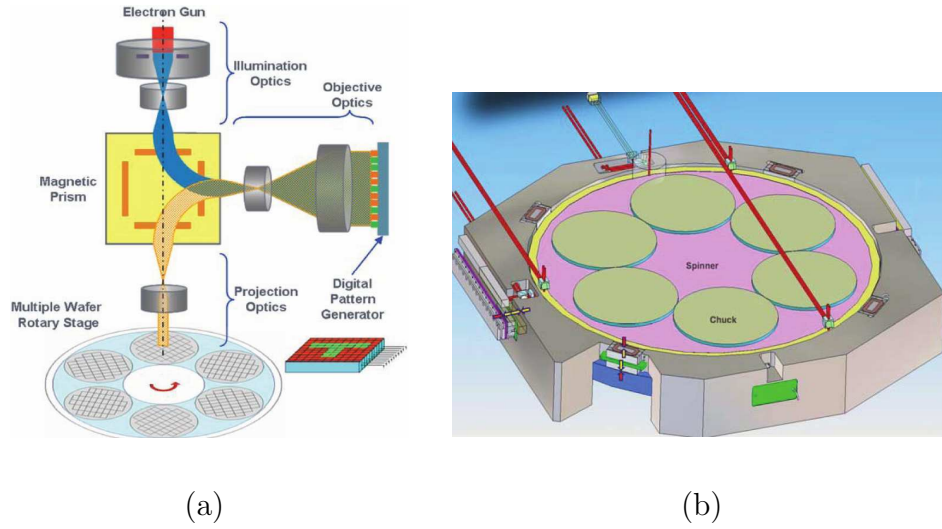


Figure 6.1: (a)Block diagram of the REBL Nanowriter; (b) detailed view of the rotary stage [33].

In the REBL system architecture, similar to the architecture presented in [12], every data path can be handled independently, with its own input data link. Moreover, in the REBL system, the DPG reads layout patterns from the decoders in a column-by-column fashion. Every decoder provides data for a fixed number of pixel rows: either 64 or 256 rows. The number of columns in each compressed 64- or 256-row “image” effectively can be thought of as being infinite, since the writing system runs continuously until the entire wafer is written. For testing purposes, we restrict the number of columns to either 1024 or 2048.

Properties of the test layout images are listed in Table 6.1.

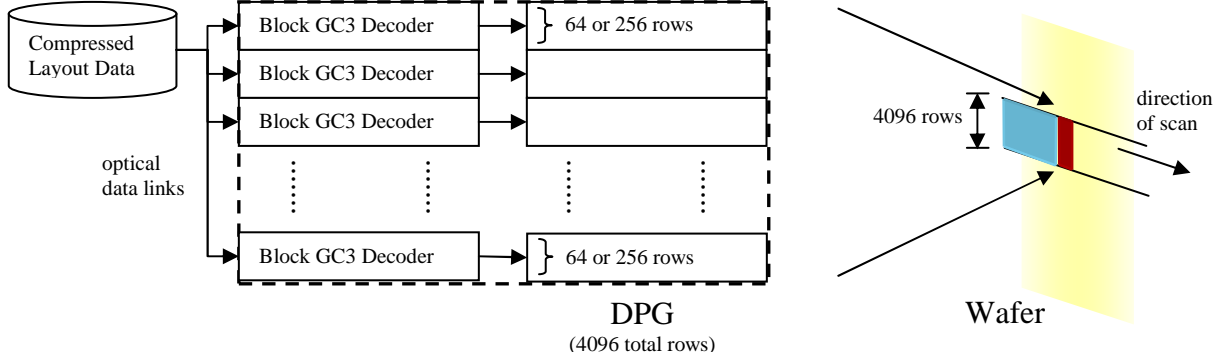


Figure 6.2: The data-delivery path of the REBL system.

Table 6.1: Properties of the test layout images.

Image Size	$64 \times 1024$ , $64 \times 2048$ , $256 \times 1024$ , $256 \times 2048$
Pixel Value	0–31 (5-bit)
Tilting Angle	25, 35

Each image pixel can take on one of 32 gray levels, in order to guarantee a 1 nm edge placement. In addition, due to the unique rotating writing stage of the REBL system, shown in Figure 6.1, the layout images are rotated at arbitrary angles, ranging from  $15^\circ$  to  $75^\circ$ . In our test set, we have collected layout images of two angles, as listed in Table 6.1. All the images have undergone E-beam proximity correction (EPC) compatible with the REBL system.

## 6.3 Adapting Block GC3 to REBL Data

In this section, we discuss the modifications that distinguish Block RGC3 from Block GC3. To ensure a feasible hardware implementation for the decoder, modifications have been added mainly to the encoding process, while keeping the decoding process as simple as possible. As shown in Sections 6.3.1 and 6.3.2, a diagonal copy algorithm and a smaller block size allow repetition in rotated layouts to be better exploited. A compression technique for segmentation information described in Section 6.3.3 reduces the impact of smaller block sizes. The tradeoff between encoding complexity and compression efficiency is discussed at the end.

### 6.3.1 Modifying the Copy Algorithm

Figure 6.3(a) shows the Block GC3 encoding process as it progresses from left to right. A history buffer stores the most recently decoded pixels, as shown in the dashed region. The current block is encoded and decoded using a strictly horizontal or vertical copy distance. Figure 6.4(a) shows an example of a 25°-rotated REBL layout image. Notice that repetition does not occur in either the horizontal or vertical direction for rotated layout images. Therefore, we need to modify the copy method to allow the decoder to copy from anywhere within the buffer range, at any arbitrary direction and distance, as shown in Figure 6.3(b). This facilitates repetition discovery regardless of the layout's angle of rotation. Note that the buffered image area does not increase for diagonal copying; however, the number of possible copy distances to choose from has increased, thereby increasing the encode complexity, as



discussed in Section 6.3.3.

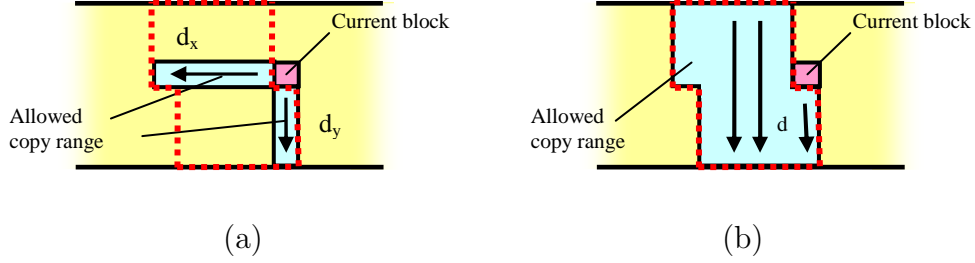


Figure 6.3: Two copy methods: (a) Block GC3: only horizontal/vertical copy is allowed; (b) Block RGC3: blocks may be copied from anywhere within the search range. In both cases, the dashed areas must be stored in the history buffer.

All results in this section refer to 25°-oriented Metal 1 layout images, which are the most challenging to compress; we assume a 40 KB buffer, which is the maximum buffer size RBEL system can afford for one data path. A performance comparison between diagonal copy and the original horizontal/vertical copy is shown in Table 6.3. As seen, for a fixed buffer size, diagonal copy improves compression efficiency by 25–70%. As compared to horizontal/vertical copying, diagonal copy decreases image errors from 17.8% to 12.1% for a 1.7 KB buffer, or from 15.9% to 6.2% for a 40 KB buffer. In other words, diagonal copy significantly improves the ability to find repetition for arbitrarily-rotated layout images.

### 6.3.2 Decreasing the Block Size

Figure 6.4(a) shows a typical rotated rasterized layout image of the REBL system. Although the image is visually repetitive, copy blocks closely approximating each  $H \times W$  image block shown in Figure 6.4(b) may not be found if the block size is too large. Thus, the block size should be sufficiently small to ensure that repetition in the image is fully exploited. How-

Table 6.2: Average compression efficiency comparison of two copy methods.

Image size	1.7 KB Buffer		40 KB Buffer	
	Hor./ Ver. Copy	Diagonal Copy	Hor./ Ver. Copy	Diagonal Copy
$64 \times 1024$	3.12	3.89	3.35	4.91
$64 \times 2048$	3.13	3.91	3.44	5.22
$256 \times 1024$	3.19	3.96	3.36	5.60
$256 \times 2048$	3.19	3.97	3.37	5.71

ever, as the block size decreases, the number of copy regions in the image tends to increase, requiring more segmentation information to be transmitted to the decoder. Specifically, reducing the block size from  $8 \times 8$  to  $4 \times 4$ , using a 40 KB buffer, reduces the image error rate from 6.2% to 2.2%<sup>1</sup>, while increasing the number of segmentation errors by a factor of 2.6.

This latter effect is aggravated by the fact that rotated layout images introduce more copy regions than  $0^\circ$ -rotated layout images, thus decreasing the effectiveness of the segmentation prediction method in [27] and also in Chapter 2. Figure 6.4(c) shows a simple example of repetition in a rotated layout image. Each pixel value represents the percentage of the pixels that lie to the right of the diagonal “edge”, which in this case is rotated by exactly  $\tan^{-1}(2)$  with respect to the pixel grid. Note that all boundary pixels can be correctly copied using a  $(d_x, d_y)$  copy distance of  $(1, 2)$ . Ignoring second-order EPC effects, the angle of rotation can

<sup>1</sup>Note that a smaller block size also implicitly requires more buffers for the region decoder in Section 4.2.2, which stores segmentation information from the previous row of blocks in order to decode the compressed segmentation values [27]. A small block size leads to more blocks per row, which increases the required buffer size. However, compared with the size of the layout image’s history buffer, especially under the 40 KB constraint, this change is negligible.

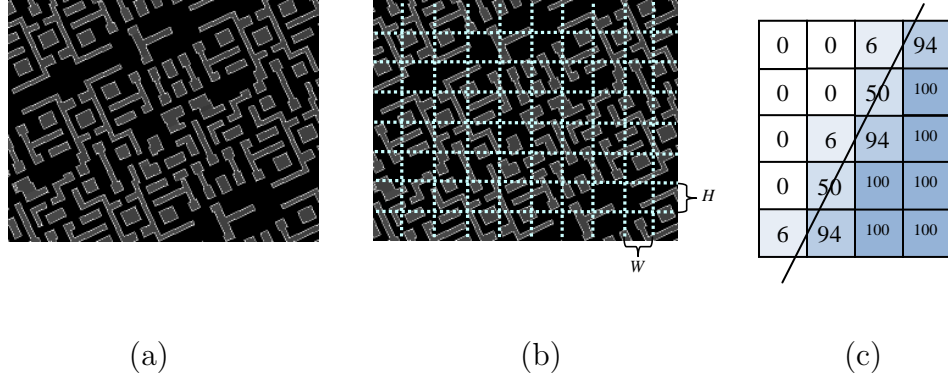


Figure 6.4: Layout image of the REBL system: (a) Original layout image; (b) fitting the image to an  $H \times W$  block grid; (c) an example of image repetition, given an edge oriented at  $\tan^{-1}(2)$  with respect to the pixel grid.

generally be approximated as  $\tan^{-1}(b/a)$ , where integers  $a$  and  $b$  are as small as possible, given the approximation remains valid; this likely leads to  $(d_x, d_y) = (a, b)$ . If  $a$  or  $b$  are too large, implementing such a large copy distance may be infeasible, due to finite buffer size, finite image width, or simply a change in the local layout feature pattern; in this case, the best copy distance may change from one block to the next. This phenomenon becomes more pronounced as the block size is reduced. Figure 6.5 shows a typical segmentation image for a  $25^\circ$ -rotated Metal 1 layout, where each pixel represents a  $4 \times 4$  block and each copy distance is randomly assigned a different color. For each block, the first-discovered copy distance resulting in minimal image errors is chosen. This segmentation map looks fairly random, making it hard to compress. In particular, after applying the segmentation prediction method in Chapter 2, only 35% of the segmentation values in Figure 6.5 are correctly predicted.

In general, encoding the segmentation map is perhaps the most challenging part of com-



Figure 6.5: Segmentation map of a  $256 \times 1024$ ,  $25^\circ$ -oriented image.

pressing REBL data using Block RGC3, especially if a small block size such as  $4 \times 4$  is used. Table 6.3 shows the percentage of each data stream after compression, using a  $4 \times 4$  block size in Block GC3. As the buffer size increases, the number of image errors decreases; however, the higher number of possible copy distances for each block results in an increase of segmentation regions. Notice that segmentation information contributes up to 76% of the total compressed data, for a 40 KB buffer size. The next subsection describes a more compression-efficient way of encoding this segmentation information. With this method in place, and assuming a square block size, we have empirically found that a  $4 \times 4$  block size optimizes compression efficiency.

Table 6.3: Bit allocation of Block GC3 compressed streams, using diagonal copying.

Buffer size	Image Error Map	Image Error Values	Seg. Error Map	Seg. Error Values
1.7 KB	28.7%	22.9%	5.2%	43.1%
20 KB	16.3%	10.9%	5.9%	66.8%
40 KB	14.5%	9.4%	5.9%	70.2%

### 6.3.3 Compression for Segmentation Information

As shown in Figure 6.5 and Table 6.3, the segmentation information looks random, and as such, could attribute to the major part of the compressed data stream. In order to improve the performance of Block RGC3, the segmentation information has to be further compressed.

There are several different approaches: First, we can apply different segmentation prediction algorithms to predict the copy distance to accommodate the angle-oriented segmentation map, as suggested in [18], [15], and [45]. However, such prediction methods may introduce extra buffers to store more than one row of blocks, and the effect can be marginal. This is again due to the randomness of the segmentation map. As a result, to maintain the simplicity of the decoder, we keep the segmentation prediction methods shown in Figure 4.5.

The next strategy is to reduce the randomness of the segmentation map, i.e., enforce the spatial coherence of the segmentation map. Notice that the map is an artificial image, and the pixel values represent different copy distances. However, for each block, there may be multiple copy distances resulting in the minimum image errors. In that sense, we can select the copy distances carefully, and grow “regions” consisting of one or more adjacent blocks, each assigned the same copy distance. By creating large regions, the segmentation map can be simplified. Regions can be grown in 2-dimensional way. The optimal region-growing metric is to minimize the total number of 2-D regions, assuming a known fixed number of image errors for each block. However, this problem is NP-complete, even if the number of image errors per block is already known, as we have shown in Appendix A. As a result, if we want to apply 2-D region growing, the heuristic algorithm again makes marginal

improvement. An alternative is to grow 1-D regions after first assuming each block contains minimal image errors; the related discussion can be found in [8] and [7].

Finally, in contrast to Block GC3, the segmentation errors in Block RGC3 have to be compressed before sending to the decoder; we apply Huffman codes to compress this. However, in this step, we split the horizontal copy distance ( $d_x$ ) and vertical copy distance ( $d_y$ ) into two streams and code them separately. The reason for this approach is simple: the size of the Huffman table is proportional to  $p \log_2 p$ , where  $p$  is the maximum value of the stream. Given a 40 KB buffer, the maximum copy distance is  $2^{16}$ , resulting in a 128 KB Huffman table, which is not practical; whereas the size of two Huffman tables with maximum copy distance  $2^8$  is 0.25 KB, which is again negligible for the REBL system. The compression efficiency of applying entropy coding is shown in Table 6.4. Notice the major improvement resulting from applying Huffman code to the segmentation information, especially for larger image sizes.

### 6.3.4 Impact on Encoding Complexity

By allowing diagonal copying, the encoder essentially compares each pixel with the pixels associated with each available copy distance. Thus, this portion of the encoding time is independent of the input image pattern. The image is both encoded and decoded in a column-by-column fashion. For Block RGC3, the number of possible copy distances per block is  $d_{x\_max} \times d_{y\_max}$ , where  $d_{y\_max}$  typically equals the height of the image and  $d_{x\_max} = buffer\_size / d_{y\_max}$ ; in contrast, for Block GC3's horizontal/vertical copying, the

Table 6.4: Compression efficiency comparison for entropy codings.

Block RGC3				
Image size	without Seg. Huffman coding		with Seg. Huffman coding	
	Avg.	Min.	Avg.	Min.
$64 \times 1024$	4.51	4.35	4.53	4.41
$64 \times 2048$	4.68	4.71	5.13	5.04
$256 \times 1024$	4.90	4.88	5.79	5.74
$256 \times 2048$	4.96	4.96	5.92	5.92

copy candidate range is  $d_{x\_max} + d_{y\_max}$ . Due to extra computational overhead which is inversely proportional to the block size, we have empirically found encoding time to vary with  $1/\beta + 1/(H \times W)$ , where  $H \times W$  represents the block size and  $\beta \approx 10$ . The  $\beta$ -dependent and block size-dependent factors equally affect encoding time when  $H \times W \approx \beta$ . Thus, Block RGC3 encoding time for a given image area is proportional to

$$O\left(d_{x\_max}d_{y\_max}\left(\frac{1}{\beta} + \frac{1}{HW}\right)\right) = O\left(buffer\_size\left(\frac{1}{\beta} + \frac{1}{HW}\right)\right).$$

Finding the best copy distance is the most time-consuming part of the encoding process, as we have shown in [8]. Table 6.5 shows samples of software encoding times for various layouts, encoding schemes, and encoding parameters, using a 2.66 GHz Intel Xeon processor with 2.75 GB RAM. The encoding times over different layers are fairly constant for Block RGC3, however, it is much greater than Block GC3. Nevertheless, if the encoding process is combined with other layout image processing techniques, such as EPC, the impact of

increasing encoding time can be minimized.

Table 6.5: Encoding times comparison between Block RGC3 and Block GC3.

Image size	Block size	Buffer size	Encoding time (sec)			
			Block GC3		Block RGC3	
			Metal 1	Via	Metal 1	Via
			25°	25°	25°	25°
$64 \times 2048$	$8 \times 8$	20 KB	0.52	0.45	28.2	28.4
$256 \times 1024$	$8 \times 8$	20 KB	0.53	0.47	66.9	62.8
$64 \times 2048$	$8 \times 8$	40 KB	0.859	0.734	49.1	49.1
$256 \times 1024$	$8 \times 8$	40 KB	0.766	0.672	124.5	116.2

## 6.4 Summary

Table 6.6 compares the compression efficiency of Block RGC3 with that of Block GC3, ZIP, BZIP2, and JPEG-LS, for 25°-oriented Metal 1 layer [48] [2] [41] [30]. Block GC3 has the buffer size of 1.7 KB and 40 KB, Block RGC3 is tested using buffer sizes of 40 KB, while ZIP, BZIP2, and JPEG-LS have constant buffer sizes of 32 KB, 900 KB, and 2.2 KB, respectively. In terms of compression efficiency, Block RGC3 consistently outperforms Block GC3, ZIP, and JPEG-LS, while BZIP2 achieves similar compression efficiency as processing the  $256 \times 2048$  image, However, impractical hardware implementation and high buffer requirements prevent BZIP2 from being a practical solution.



Table 6.6: Compression efficiency comparison of different compression algorithms.

Image size	Compression method						
	Block GC3		Block RGC3		ZIP	BZIP2	JPEG-LS
	Avg.(1.7 KB)	Avg.(40 KB)	Avg.	Min.	(32 KB)	(900 KB)	(2.2 KB)
$64 \times 1024$	3.03	3.36	4.53	4.41	3.53	3.70	0.94
$64 \times 2048$	3.04	3.44	5.13	5.54	3.78	3.95	0.95
$256 \times 1024$	3.11	3.37	5.79	5.74	4.03	4.48	0.96
$256 \times 2048$	3.11	3.37	5.92	5.92	4.11	4.69	0.97

Table 6.7 shows the compression efficiency of Block RGC3 over different layers and angles. It is obvious that the  $25^\circ$  Metal 1 image is the most challenging one to compress, and the  $25^\circ$  angle is the most challenging angle to compress throughout our test images. The Via layer, most likely to be the layer to apply direct-write lithography in the next generation, achieves an average compression ratio above 14, which satisfies the requirement of the REBL system. In fact, all of our test images meet the minimum compression ratio of 5 requirement. However, these images are fairly sparse, with the feature density shown in Table 6.7. A more dense image may result in a much lower compression ratio, and therefore a more extensive investigation of different layouts is needed to characterize the performance of Block RGC3.

Table 6.7: Block RGC3 Compression efficiency comparison of different layout images.

Layer	Angle	Compression ratio	Layout density (%)
Poly	35°	10.97	20.2
Metal 1 Control	25°	12.30	31.2
Metal 1 Memory	25°	5.79	38.1
	35°	6.13	38.1
Via	25°	14.56	4.4
	35°	14.88	4.4

## Chapter 7

# Conclusions and Future Work

Maskless lithography has been proposed as an alternative to optical lithography in order to reduce the cost of the mask sets. However, to realize this direct-write technique, several issues need to be addressed, including manufacturing micromirror array writing system using MEMS, correcting proximity effect causing by the EUV and E-beam sources, controlling the sources with desired degrees of freedom, actuating the micromirror array using mix signal circuits, etc. Among them, the data delivery problem, transmitting the data from external storage devices to the writer system for real-time update, is a bottleneck for realistic data throughput of direct-write lithography systems. To this end, we have proposed to losslessly compress the data beforehand, transmit the compressed data, and decompress it on-the-fly in the writer chip. This implies the compression algorithm has to be asymmetric, i.e., the decoder has to be simple and implementable in hardware with minimal overhead, while the overall compression efficiency must be large enough to reduce the transmission and storage

overhead to a manageable level.

In this thesis, I have presented a lossless compression algorithm, Block Golomb Context-Copy Code (GC3), that is implementable in hardware. The compression efficiency of Block GC3 outperforms all existing lossless data compression algorithms, including LZ, ZIP, BZIP2, JPEG-LS, Huffman, and run-length coding, with the decoder buffer of only 1.7 KB. Although it has a 10–15% efficiency loss as compared to the previously proposed Block C4 algorithm, I have shown Block GC3 achieves a much simpler hardware decoder design, thus compensating for the compression efficiency loss.

I also have presented hardware design for Block GC3 decoder, along with the FPGA and ASIC synthesis and simulation results. I have shown that Block GC3 results in a simple digital circuit. A single Block GC3 decoder only utilizes 4% of the resources of a Xilinx Virtex Pro II 70 FPGA. The system can run at 100 MHz, resulting in an output data rate of 495 Mb/s. Meanwhile, the corresponding ASIC synthesis in the 65 nm technology results in an area of  $0.07\text{mm}^2$  with the maximum output data rate of 2.47 Gb/s for a single decoder. For 200 decoders running in parallel, resulting in the total output data rate of 500 Gb/s, or 3 wafer layers per hour, the required area and power are  $14\text{mm}^2$  and 5.4 W respectively. As compared to the direct-write method, this results in a power saving of 24% with a minimal amount of hardware overhead [4]. With these synthesis results and data-flow architecture of the decoder, it is potentially feasible to run hundreds Block GC3 decoders in parallel to achieve the high-throughput needed for direct-write lithography systems.

To integrate the decoder into the writer chip, I have proposed several data handling

strategies for the data path. Regarding on-chip input FIFO buffering, the input data rate can be reduced with a smaller memory as compared to our previous work [10], by utilizing the simultaneous read/write property of FIFO. Meanwhile, with additional output data buffering, the data between multiple decoders and writer devices can be synchronized, so that multiple decoders can run in their own data flow without jeopardizing the final output. In addition, error propagation control techniques such as memory refreshing and Hamming code are introduced to minimize the impact of error propagation caused by imperfect data retention ability of the memory. Finally, input data stream packaging is proposed to reduce the number of input data streams, which can also reduce the I/O complexity if multiple decoders are applied. This hardware data path implementation is independent of the writer systems or data link types, and can be integrated with arbitrary direct-write lithography systems.

To investigate the integration of Block GC3 with a real direct-write lithography system, I have applied Block GC3 to the reflective electron-beam lithography (REBL) system, developed by KLA-Tencor [33] [32]. Two characteristic features of the REBL system are a rotary stage resulting in arbitrarily-rotated layout imagery, and E-beam corrections prior to writing the data, both of which present significant challenges to lossless compression algorithms. Together, these effects reduce the effectiveness of both the copy and predict compression methods within Block GC3.

To deal with these challenges, I have proposed technique Block RGC3, which divides the image into a grid of two-dimensional “blocks” of pixels, each of which is copied from a

specified location in a history buffer of recently-decoded pixels. However, in Block RGC3 the number of possible copy locations is significantly increased, so as to allow repetition to be discovered along any orientation, rather than horizontal or vertical. Also, by copying smaller groups of pixels at a time, repetition in layout patterns is easier to be found and taken advantage of. As a side effect, this increases the total number of copy locations to transmit; to overcome this, I have presented several strategies to reduce the transmitted data volume, thereby improving compression efficiency. I have characterized the performance of Block RGC3 in terms of compression efficiency and encoding complexity on a number of rotated Metal 1, Poly, and Via layouts at various angles, and shown that Block RGC3 provides higher compression efficiency than existing lossless compression algorithms for rotated layouts.

Through this work, I have presented Block GC3 as a solution for the data delivery issue of direct-write lithography systems. However, since Block GC3 is a generic lossless compression algorithm for direct-write lithography systems, the algorithm may need to be modified to accommodate the specifics of different writer technologies and layout images while keeping the decoder complexity low. Extensive testing over different layouts and layers is needed when specifically targeting a given writing system [47].

The integration of decoder and writer chip poses additional challenges. For example, we need to investigate the scalability and multi-thread data handling issues of the parallel decoding systems when hundreds of decoders are on the same chip. In this case, it is impossible to manually place the memory blocks at the floor-planning stage, and therefore an automatic system or a inter-core memory sharing strategy is needed.

On the algorithmic side, Block GC3 also leaves some open questions. For example, can we find a better segmentation algorithm to reduce the number of copy regions? In addition, after we find a segmentation, is there a better way to code it so the size of the compressed data can be reduced? The 1-D region growing method in [8] provided a possible solution to reduce the complexity of the segmentation map; however, a generalized two-dimensional solution and a better data representation algorithm may still improve the compression efficiency.

Besides direct-write lithography application, the lossless compression algorithm can also be applied to compress natural images and videos, as needed in the film and medical imaging industries. However, since Block GC3 adapts some major characteristics of the layout images to achieve the best compression efficiency, the algorithm can not be applied to natural images directly. Developing a low-decoding complexity algorithm for natural images can also be a very interesting topic.

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# Appendix A

## Proof of NP-Completeness for

## Two-Dimensional Region

## Segmentation

Assume that each block is given a list of copy distances which yield no more than some pre-determined number of image errors, as described in Chapter 6. In this Appendix, we show that the process of choosing one copy distance from each block's list such that the total number of regions is minimized is NP-complete. We define a "region" as a group of 4-connected blocks each having the same copy distance. Let  $X_1$  be an image with  $n$  optimal copy distances  $D(p) = \{d_1(p), d_2(p), \dots, d_n(p)\}$  for all blocks  $p \in X_1$ . Our goal is to minimize the number of regions in  $X_1$ , such that each block in a given region has at least one copy

distance in common. More formally, the following uniformity predicate holds:

$$U_1(X_1) = \text{true iff } \forall p \in X_{1,i}, \exists a \text{ s.t. } a \in D(p),$$

where  $X_{1,i}$  is any region in  $X_1$ . As proven by MIN2DSEG in [5], minimizing the number of 2-D regions in an image  $X_2$  is an NP-complete problem, assuming the uniformity predicate

$$U_2(X_2) = \text{ture iff } \forall p, q \in X_{2,i}, |I(p) - I(q)| \leq 1,$$

where  $I(p)$  are the block values for all blocks  $p \in X_2$ . For  $X_2$ , let  $D(p) = \{I(p), I(p) + 1\}$ .

$U_1(X_2)$  and  $U_2(X_2)$  are equivalent; this proves the reduction from MIN2DSEG in [5] to our 2-D region-segmentation method, which is thus NP-complete.



## Appendix B

### Schematics of Block GC3 Decoder

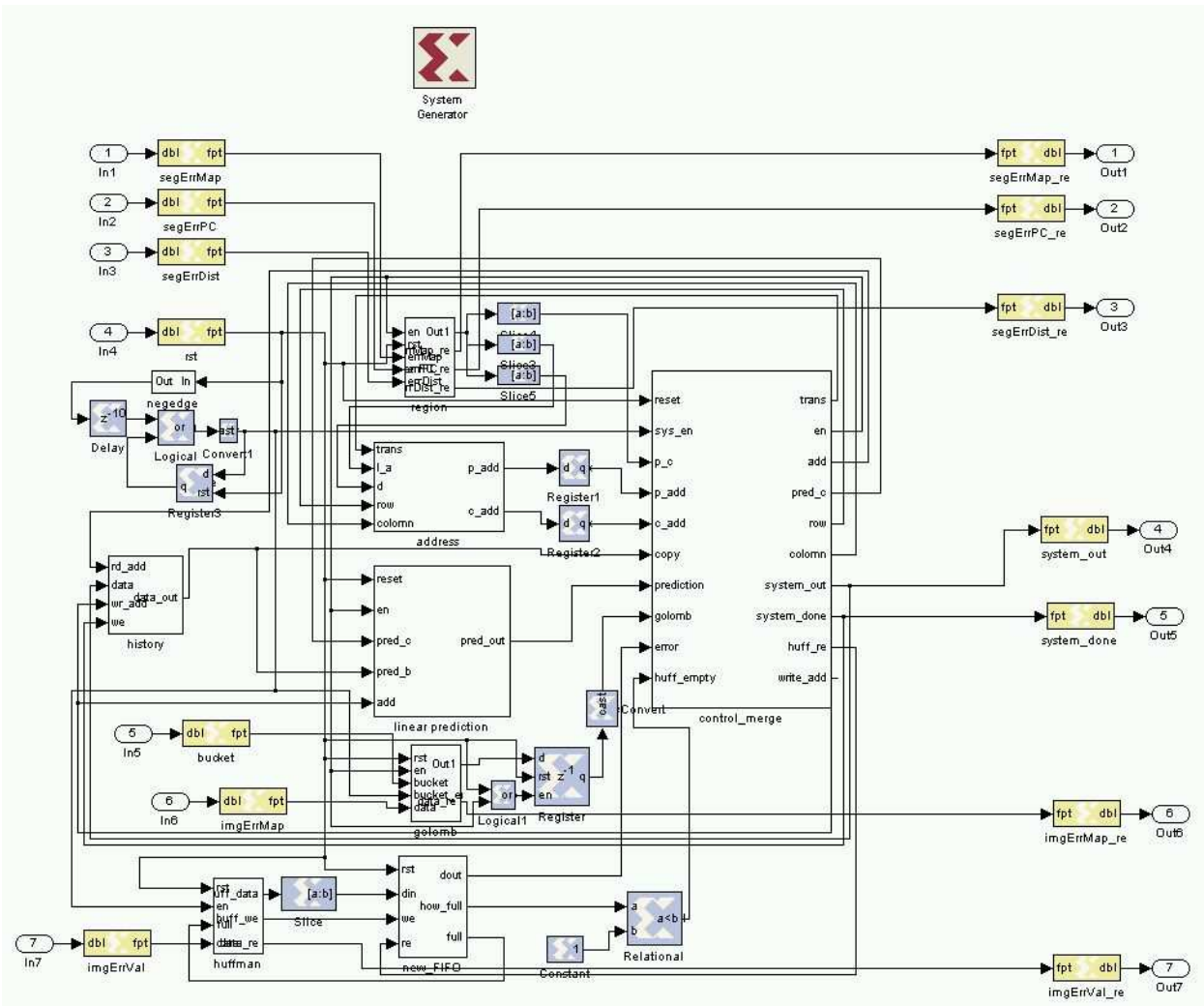


Figure B.1: The block diagram of BlockGC3 decoder.

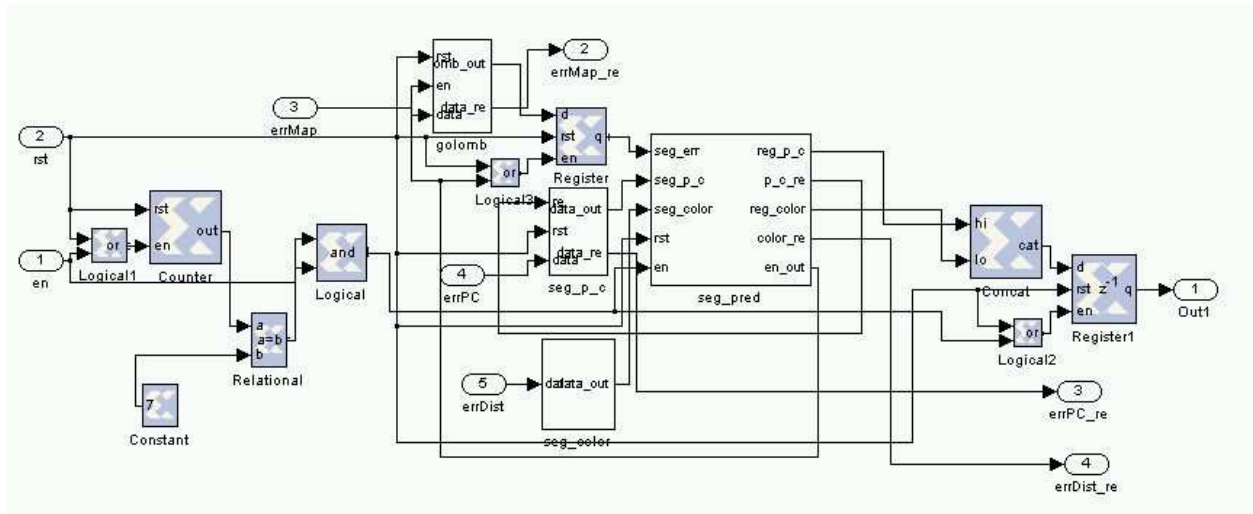


Figure B.2: The block diagram of region decoder.

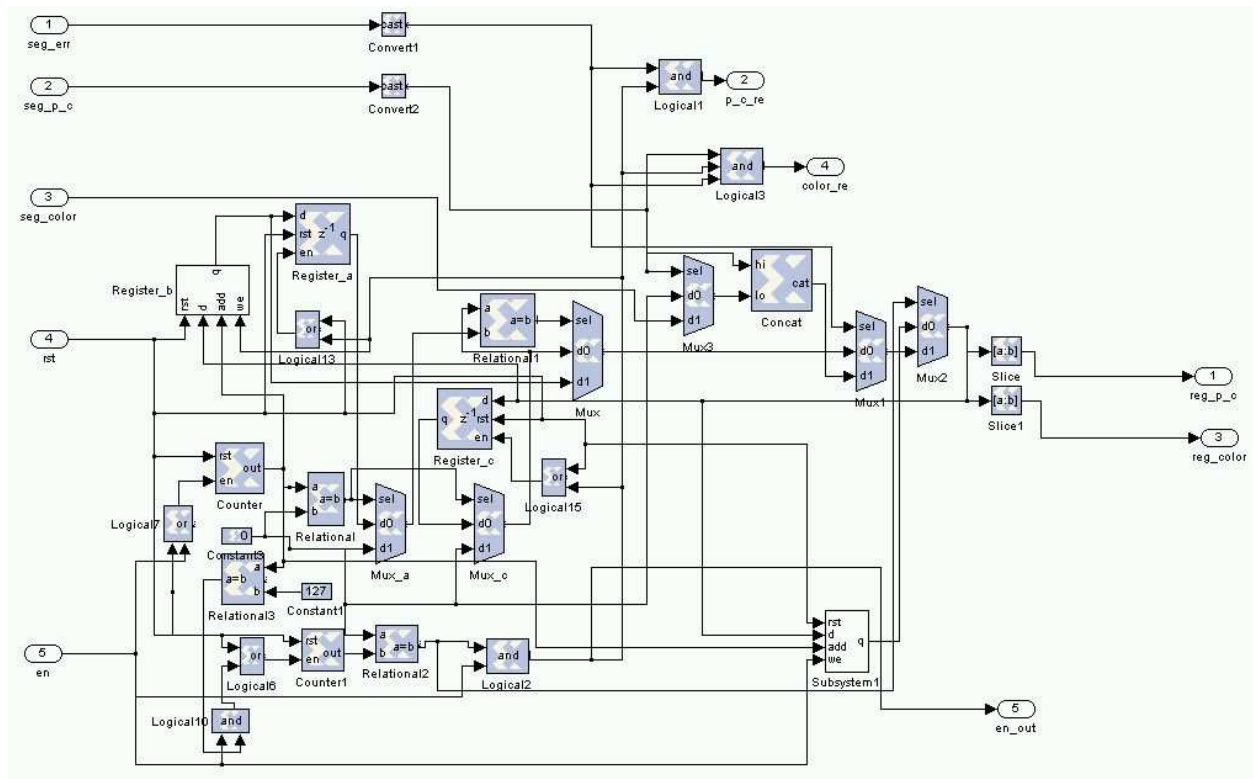


Figure B.3: The block diagram of the segmentation predictor.

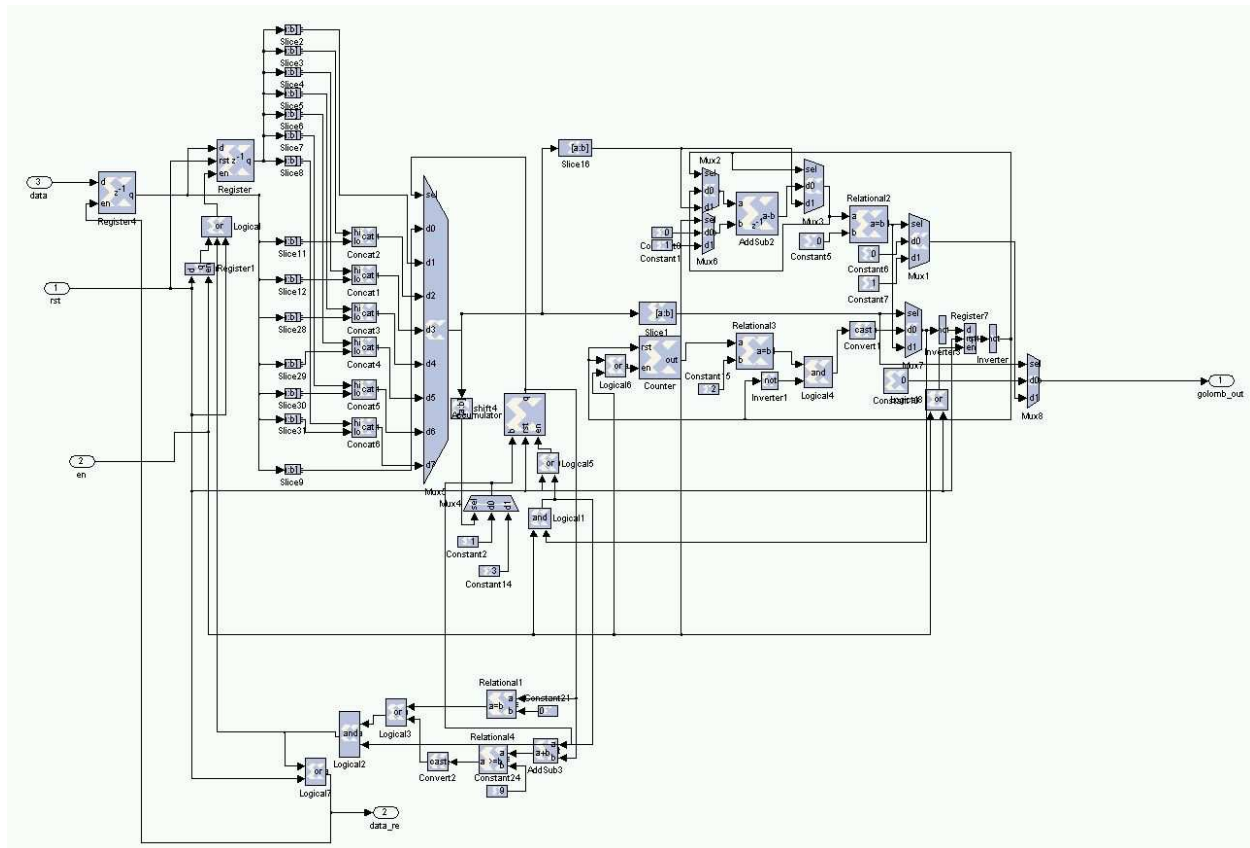


Figure B.4: The block diagram of Golomb run-length decoder for region decoder.

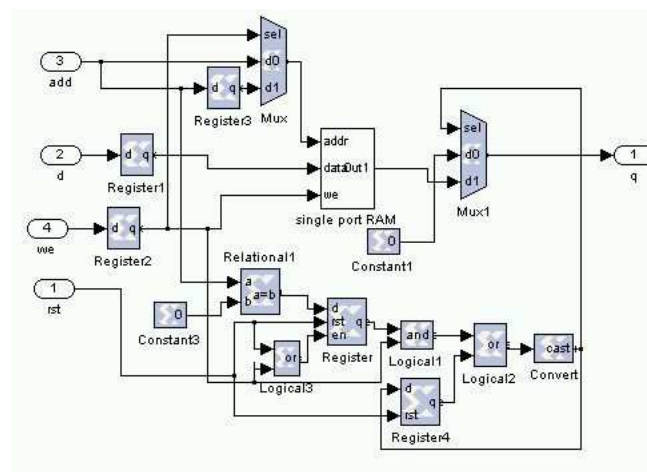


Figure B.5: The block diagram of the delay chain.

Figure B.6: The block diagram of linear predictor.

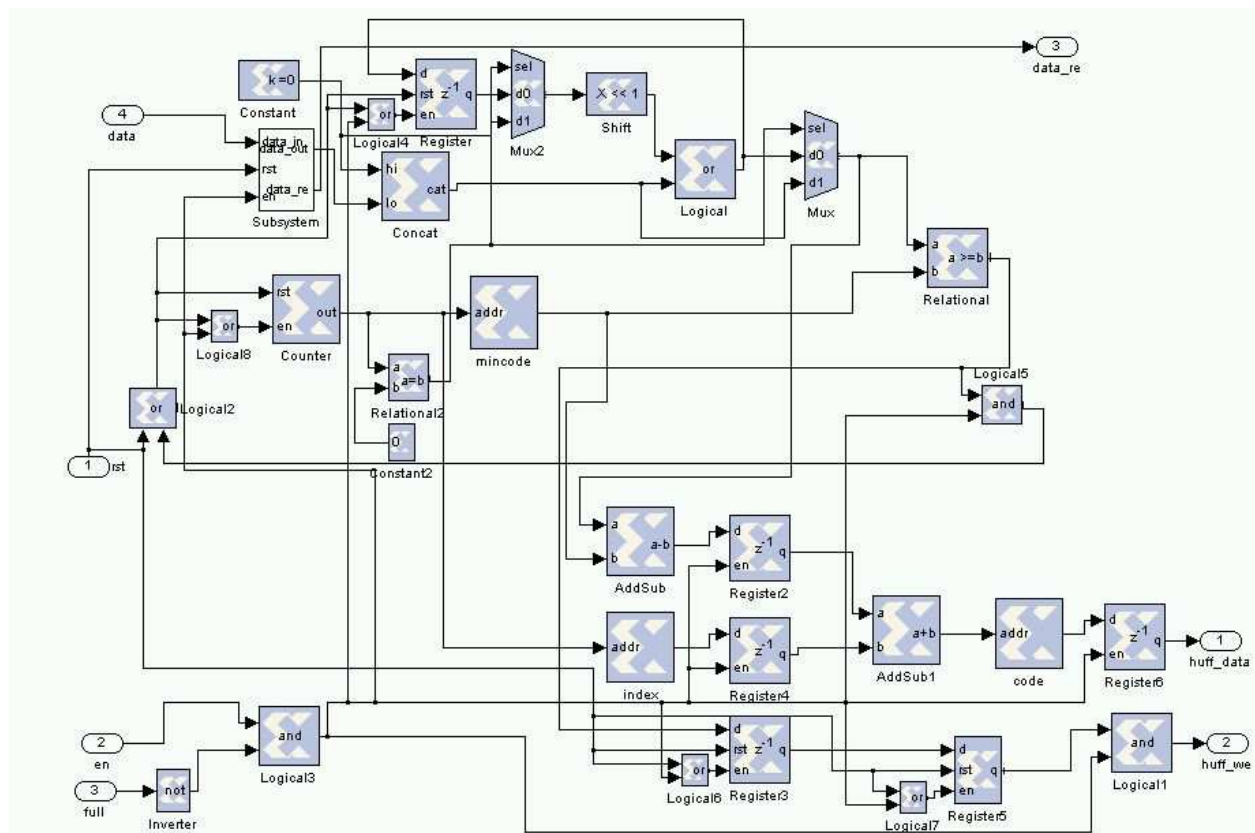


Figure B.7: The block diagram of Huffman decoder.

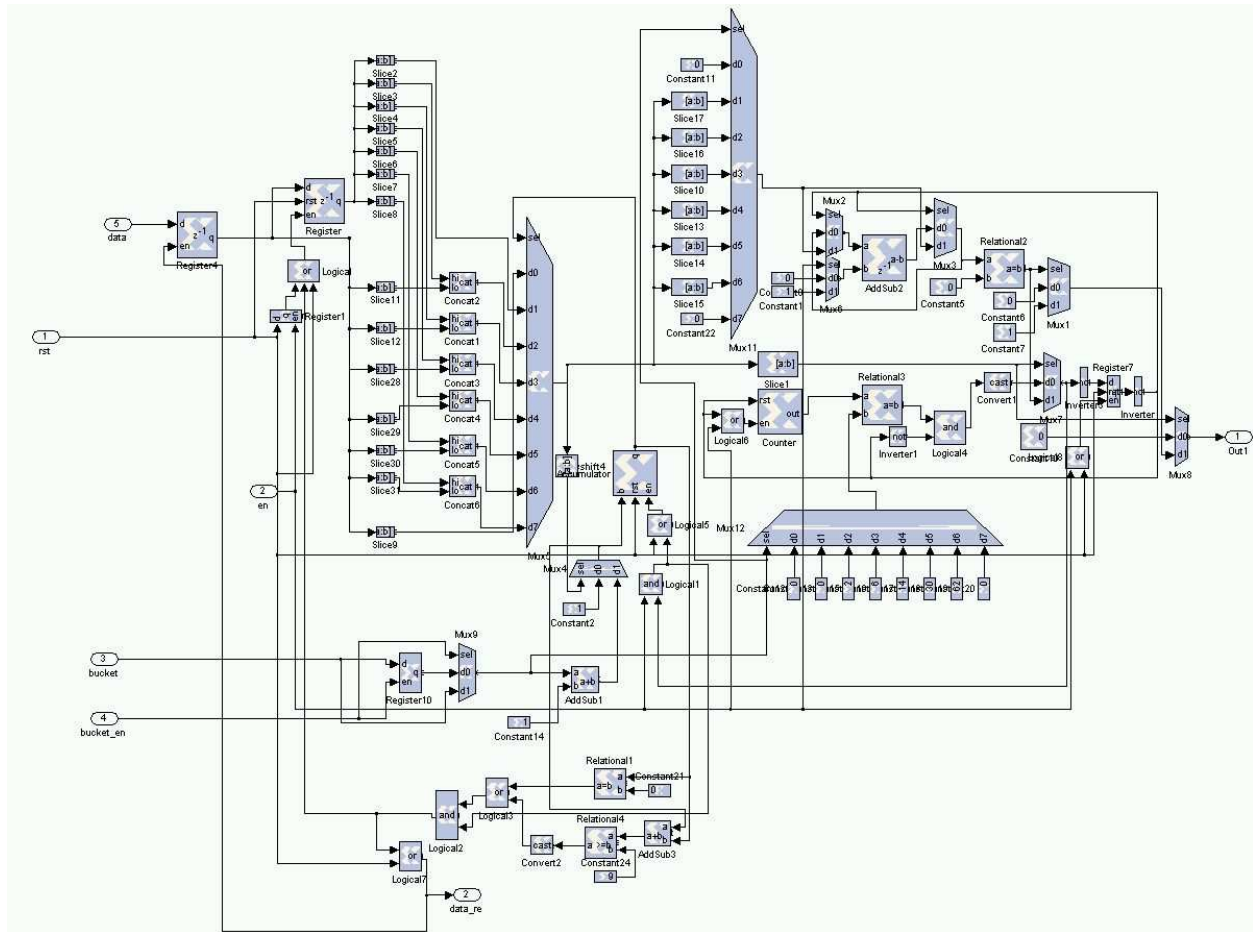


Figure B.8: The block diagram of Golomb run-length decoder for image error location.

Figure B.10: The block diagram of the history buffer.



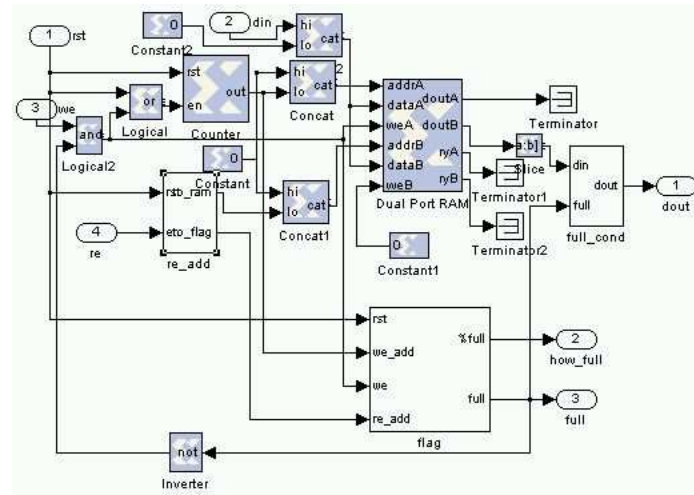


Figure B.11: The block diagram of FIFO.

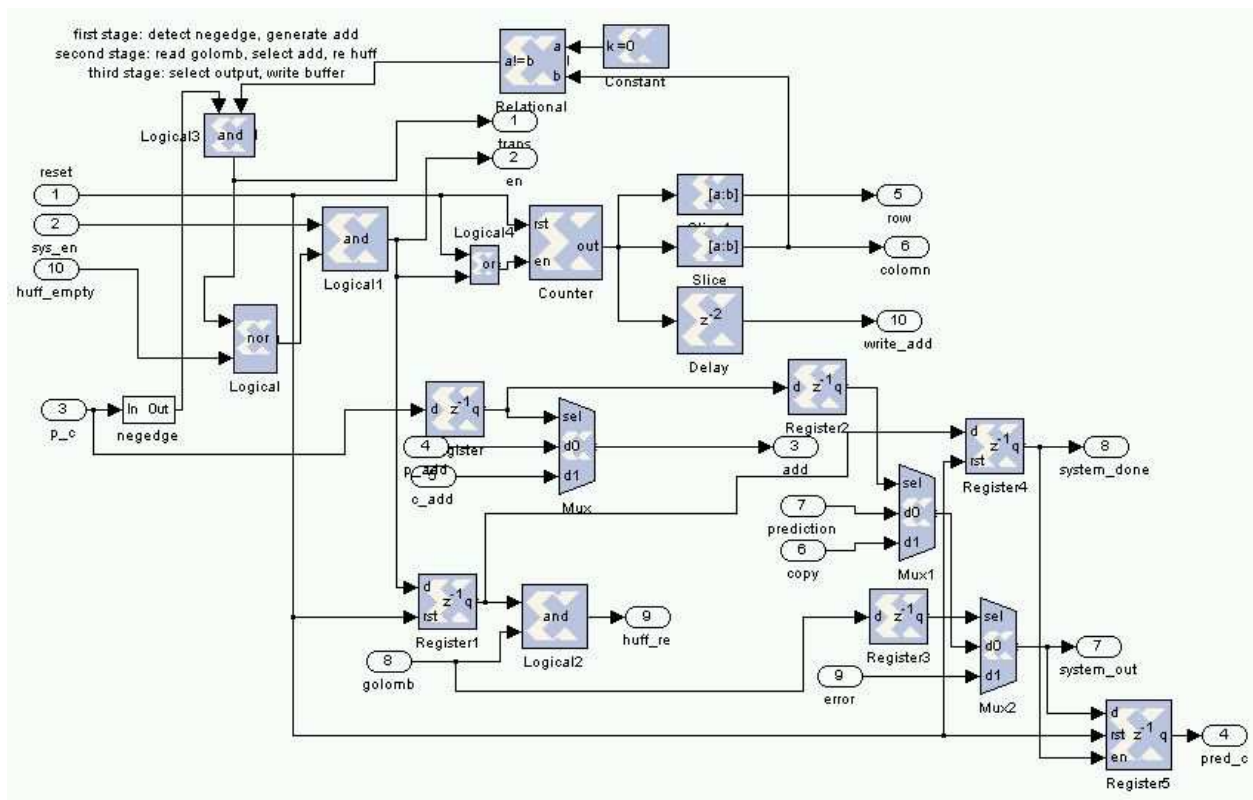


Figure B.12: The block diagram of the control block.